



**ANSI/ASHRAE Standard 96-1980(RA89) (W)**

**Intent to Withdraw**

# **Methods of Testing to Determine the Thermal Performance of Unglazed Flat-Plate Liquid-Type Solar Collectors**

**First Withdrawal Review (October 2024)**

This standard will be submitted to the American National Standards Institute Board of Standards Review (BSR) with a notice of Intent-to-Withdraw.

This intent-to-withdraw draft has been recommended for public review by the cognizant technical committee and approved by a subcommittee of the Standards Committee. To submit a comment on this proposed withdrawal, go to the ASHRAE website at <http://www.ashrae.org/technology/page/331> and access the online comment database. The draft is subject to modification until it is approved for publication by the ASHRAE Board of Directors and ANSI. Until this time, the current edition of the standard (as modified by any published addenda on the ASHRAE Web site) remains in effect. The current edition of any standard may be purchased from the ASHRAE Bookstore at [www.ashrae.org](http://www.ashrae.org) or by calling 404-636-8400 or 1-800-527-4723 (for orders in the U.S. or Canada).

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## CONTENTS

### ASHRAE Standard 96-1980 (RA 1989), Methods of Testing to Determine the Thermal Performance of Unglazed Flat-Plate Liquid-Type Solar Collectors

SECTION	PAGE
Foreword.....	3
Nomenclature.....	3
1 Purpose .....	3
2 Scope .....	3
3 Definitions.....	3
4 Classifications.....	4
5 Requirements .....	4
6 Instrumentation.....	5
7 Apparatus and Method of Testing .....	6
8 Test Procedure and Computations.....	9
9 Data to be Recorded and Test Report.....	14
10 References .....	16
Test Report Table 1 .....	14
Test Report Table 2 .....	14
Appendix A .....	16
Appendix B .....	17
Appendix C .....	27

#### NOTE

Approved addenda, errata, or interpretations for this standard can be downloaded free of charge from the ASHRAE Web site at [www.ashrae.org/technology](http://www.ashrae.org/technology).

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## FOREWORD

This Standard describes tests for determining the thermal performance of unglazed collectors used in low temperature applications such as heating of swimming pools and with heat pumps. Glazed and/or concentrating collectors used in these same applications are intended to be tested for thermal performance in accordance with ASHRAE Standard 93-1986.

It should be recognized that the thermal performance of a single collector may not be indicative of the performance of a collector array consisting of a number of modules of the same collector.

The 1980 Standard was recommended for reaffirmation with minor editorial changes by the Standards Committee on June 28, 1987. Since the ASHRAE Journal intent-to-reaffirm notice elicited no negative comments, the Board of Directors approved the reaffirmation with minor editorial changes on February 2, 1989.

## 1.0 PURPOSE

**1.1** The purpose of this Standard is to provide test methods for determining the thermal performance of unglazed flat-plate liquid-type solar energy collector modules (hereinafter called solar collectors) which heat a liquid for low temperature applications.

## 2.0 SCOPE

**2.1 Application.** This Standard applies to unglazed flat-plate liquid-type solar collectors to be used in low temperature applications and in which a liquid enters the collector through a single inlet and leaves the collector through a single outlet.

**2.1.1** Collectors containing more than one inlet and more than one outlet may be tested according to this Standard provided that the external piping can be connected so as to provide effectively a single inlet and a single outlet.

**2.1.2** Collectors, other than unglazed flat-plate liquid-type, which are intended for low temperature applications should be tested in accordance with ASHRAE Standard 93-1986 modified in accordance with the requirements of Section 8.3 of this Standard.

**2.2 Outdoor and Indoor Testing.** This Standard contains methods for conducting tests outdoors under natural solar irradiation and for conducting tests indoors under simulated solar irradiation.

**2.3 Test Methods and Calculation Procedures.** This Standard provides test methods and calculations procedures for determining steady-state and quasi-steady-state thermal performance, and angular response characteristics of the solar collectors.

## NOMENCLATURE

a,b	= constants used in incident angle modifier equation, dimensionless
A <sub>a</sub>	= transparent frontal area or aperture area for a flat-

A <sub>g</sub>	= plate collector, m <sup>2</sup> (ft <sup>2</sup> )
b <sub>o</sub>	= gross collector area, m <sup>2</sup> (ft <sup>2</sup> )
c <sub>p</sub>	= constant used in incident angle modifier equation, dimensionless
F <sub>R</sub>	= specific heat of the transfer fluid, J/(kg· °C) [Btu/(lb· °F)]
I <sub>DN</sub>	= solar collector heat removal factor, dimensionless
I <sub>d</sub>	= direct normal solar irradiation, W/m <sup>2</sup> [Btu/(h· ft <sup>2</sup> )]
I <sub>sc</sub>	= diffuse solar irradiation incident upon the aperture plane of collector, W/m <sup>2</sup> [Btu/(h· ft <sup>2</sup> )]
I <sub>t</sub>	= solar constant, 1353 W/m <sup>2</sup> [429.2 Btu/(h· ft <sup>2</sup> )]
K <sub>art</sub>	= total solar irradiation incident upon the aperture plane of collector, W/m <sup>2</sup> [Btu/(h· ft <sup>2</sup> )]
LST	= incident angle modifier, dimensionless
LSTM	= local standard time, decimal hours
AST	= local standard time meridian, deg
ṁ	= apparent solar time, decimal hours
P <sub>th</sub>	= mass flow rate of the transfer fluid, kg/s (lb/h)
Δp	= theoretical power required to move the transfer fluid through the collector, W (hp)
q <sub>u</sub>	= pressure drop across the collector, Pa (lb/in. <sup>2</sup> )
t <sub>a</sub>	= rate of useful energy extraction from the collector, W(Btu/h)
t <sub>f,e</sub>	= ambient air temperature, °C (°F)
t <sub>f,i</sub>	= temperature of the transfer fluid leaving the collector, °C (°F)
t <sub>p</sub>	= temperature of the transfer fluid entering the collector, °C (°F)
Δt	= average temperature of the absorber surface for a flat-plate collector, °C (°F)
U <sub>L</sub>	= temperature difference, °C (°F)
w	= solar collector heat transfer loss coefficient, W/(m <sup>2</sup> · °C) [Btu/(h· ft <sup>2</sup> · °F)]
α	= density, kg/m <sup>3</sup> (lb/ft <sup>3</sup> )
θ	= absorptance of the collector absorber surface for solar radiation, dimensionless
n <sub>g</sub>	= angle of incidence between direct solar rays and the normal to the collector surface or to the aperture, deg
λ	= collector efficiency based on gross collector area, %
τ	= wavelength, μm
(τα) <sub>e</sub>	= transmittance of the solar collector cover plate, dimensionless (if no cover plate is used, τ = 1.0)
(τα) <sub>e,n</sub>	= effective transmittance-absorptance product, dimensionless
T <sub>1,T<sub>2</sub></sub>	= effective transmittance-absorptance product at normal incidence, dimensionless
T <sub>1,T<sub>2</sub></sub>	= time at the beginning and end of a test period, decimal hours

## 3.0 DEFINITIONS

**absorber:** that part of the solar collector which receives the incident radiant energy and transforms it into thermal energy. It may possess a surface through which energy is transmitted to the transfer liquid; however, the transfer liquid itself can be the absorber.

**absorber area:** the total heat transfer area through which the absorbed solar irradiation heats the transfer liquid or of the absorber media if both transfer liquid and solid surfaces jointly perform the absorbing function.

**air mass:** the ratio of the mass of atmosphere in the actual earth-sun path to the mass which would exist if the sun were directly overhead at sea level.

**angle of incidence:** the angle between the direct solar beam and the normal to the aperture plane.

**aperture area:** the maximum projected area of a solar collector through which the unconcentrated solar radiant energy is admitted.

**area, gross collector:** the maximum projected area of the complete collector module exclusive of integral mounting means and liquid connectors. For assemblies of collectors, gross area includes the entire area of the assembly.

**collector, unglazed:** a solar collector in which the absorbing surface is directly exposed to the atmosphere.

**collector, flat-plate:** a non-concentrating solar collector in which the absorbing surface is essentially planar.

**collimation angle:** the angle within which the radiation beams from the source depart from the line drawn from the source to the receiver.

**insolation:** see Irradiation, Instantaneous.

**irradiation, instantaneous:** the total quantity of solar radiation incident on a unit surface area in unit time, measured in  $\text{W/m}^2$  ( $\text{Btu}/(\text{h} \cdot \text{ft}^2)$ ).

**instantaneous efficiency:** the amount of energy removed by the transfer liquid per unit of gross collector area during the specified time period divided by the total solar radiation incident on the collector per unit area during the same time period, under steady-state or quasi-steady-state conditions.

**pyranometer:** a radiometer used to measure the total solar radiation incident upon a surface per unit time per unit area. This energy includes the direct radiation, the diffuse sky radiation, and the solar radiation reflected from the foreground.

**pyrheliometer:** a radiometer used to measure the direct radiation on a surface normal to the sun's rays.

**quasi-steady-state:** describes the state of the solar collector test when the flow rate and temperature of the liquid entering the collector are constant but the exit fluid temperature changes gradually due to the normal change in irradiation that occurs with time for clear sky conditions.

**solar collector:** a device designed to absorb incident solar radiation and to transfer the energy to a liquid passing through it.

**temperature, ambient air:** the temperature of the air surrounding the solar collector being tested.

**transfer liquid, heat:** the medium which passes through the solar collector and carries the absorbed thermal energy away from the collector.

## 4.0 CLASSIFICATIONS

**4.1 Basis of Classifications.** Solar collectors may be classified according to their collecting characteristics, the way in which they are mounted, the type of transfer liquid, and the flow direction which they employ.

**4.1.1 Collecting Characteristics.** An unglazed flat-plate collector is one in which the absorbing surface is directly exposed to the atmosphere, where the absorbing surface is essentially flat, and in which the aperture and the absorber are similar in area and geometry. Other types include glazed (single or multiple) and/or concentrating collectors.

**4.1.2 Mounting.** A solar collector may be mounted in a stationary position with a fixed azimuth and tilt angle (measured from the horizontal) or it may be adjustable as to tilt angle to follow the annual changes in solar declination.

**4.1.3 Type of Liquid.** In low temperature applications, collectors normally employ water circulated directly through the passages in the collector. They may however, employ a heat transfer liquid and a heat exchanger to heat the water.

**4.1.4 Flow Direction.** The liquid may flow in any manner through the collector. Figures 1, 2 and 3 show flow from bottom to top.

## 5.0 REQUIREMENTS

**5.1 General.** Unglazed flat-plate liquid-type solar collectors shall be tested in accordance with the provisions set forth in this Section and in Section 8.

**5.1.1 Preconditioning.** The collector whose thermal performance is to be tested in accordance with this document shall be preconditioned prior to initiation of the test. Preconditioning shall consist of stagnation heating in a non-operational mode in a dry condition for not less than three days (not necessarily successive) in which the cumulative mean incident solar radiation measured in the plane of the collector shall be not less than  $17,000 \text{ kJ}/(\text{m}^2 \cdot \text{day})$  ( $1500 \text{ Btu}/(\text{ft}^2 \cdot \text{day})$ ). The exposure angle shall be the angle of test specified herein.

**5.1.2 Size of Test Sample.** Testing of full scale modules is preferred. The size of the collector to be tested shall be large enough so that the performance characteristics determined will be indicative of those that would occur when the collector is part of an installed system. If the collector is modular and the test is being done on one module, it should be mounted and insulated in such a way that the back and edge losses will be characteristic of those that will occur during operation on a structure. If special liquid connectors are furnished or required by the manufacturer of the collector, they shall be used for introducing the fluid during testing. If the manufacturer recommends or furnishes a special panel inter-connection means, a stub-off unit shall be installed on the panel during testing.

**5.1.3 Collector Mounting.** If the collector module is designed with no back insulation, for test it shall be mounted on a rigid insulating board having an insulating value of  $R = 0.88 \text{ m}^2 \cdot ^\circ\text{C}/\text{W}$  ( $5.0 \text{ ft}^2 \cdot \text{h} \cdot ^\circ\text{F}/\text{Btu}$ ).

**5.1.4 Avoidance of Reflected Radiation.** For tests conducted outdoors to determine thermal efficiency and incident angle modifier, the collector shall be mounted in a location such that there will be no significant energy reflected or reradiated onto the collector from surrounding buildings or any other surfaces in the vicinity of the test stand for the duration of the test(s). This requirement will be satisfied if the ground and immediately adjacent foreground surfaces are diffuse reflectors with a reflectance of less than 0.20. If significant reflection can occur, provision shall be made to shield the collector by the use of a non-reflective shield. In addition, the test stand shall be located so that no shadow will be cast onto the collector by any obstruction at any time during the test period.

**5.1.5 Weather Conditions.** For tests conducted outdoors to determine thermal efficiency, the tests shall be

conducted at times having weather conditions such that the integrated average irradiation measured in the plane of the collector or aperture, reported, and used for the computation of instantaneous efficiency values shall be not less than  $630 \text{ W/m}^2$  [200 Btu/(h · ft $^2$ )]. Specific irradiation values that can be expected for clear sky conditions are shown in Tables B1 through B6 taken from Ref. 1. More accurate estimates can be made using the tables in conjunction with Clearance Numbers (see Ref. 2, pg. 27.3, Fig. 3).

**5.1.6 Orientation.** For tests conducted to determine thermal efficiency at near normal incidence conditions, the orientation of the collector shall be such that the incident angle (measured from the normal to the collector surface or aperture) is less than  $30^\circ$  during the period in which test data are being taken. Angle of incidence may be estimated from Tables B7 through B12 taken from Ref. 3. More accurate estimates can be made using the procedures outlined in Refs. 2, pg. 27.3; and 4, Chapter 58.

**5.1.7 Collector Surface Air Speed.** For tests conducted to determine thermal efficiency and incident angle modifier, the average air speed across the collector surface shall be measured and recorded for each data point. Measurements shall be made in the immediate vicinity of the collector, at a height not greater than 15.3 cm (6 in.) above the surface of the collector and at locations where the wind speed sensor is not shielded from the wind and the sensor does not significantly cast a shadow on the collector during the tests. Average wind speed for each data point shall not exceed 1.3 m/s (3.0 mph).

**5.1.8 Ambient Temperature Range.** For tests conducted outdoors to determine collector thermal efficiency, the range of ambient temperatures for all reported test points comprising the efficiency curve shall be less than  $10^\circ\text{C}$  ( $18^\circ\text{F}$ ) and in the range of 15 to  $38^\circ\text{C}$  (60 to  $100^\circ\text{F}$ ).

**5.1.9 Transfer Liquid Specific Heat and Density.** The transfer liquid used in the solar collector shall have known specific heat which varies by less than 0.5% in the temperature range of the liquid during a particular test period. The density of the transfer liquid shall also be known and it shall not vary by more than 0.5% over a particular test period.

## 6.0 INSTRUMENTATION

### 6.1 Solar Radiation Measurement.

**6.1.1 Total Irradiation Measurement.** A pyranometer shall be used to measure the total short wave radiation from both the sun and the sky. A pyrheliometer may be used to measure the direct normal radiation. The instruments shall have the following minimum characteristics, which are consistent with current practice or requirements of a first class pyranometer (or pyrheliometer if used) as classified by the World Meteorological Organization (WMO)<sup>5-7</sup>:

**6.1.1.1 Change of Response Due to Variation in Ambient Temperature.** The instruments shall be equipped with a built-in temperature compensation circuit and have a temperature sensitivity of less than  $\pm 1\%$  over the range 15 to  $38^\circ\text{C}$  (60 to  $100^\circ\text{F}$ ).

**6.1.1.2 Variation in Spectral Response.** Pyranometer and pyrheliometer errors caused by a departure from the required spectral response of the sensor shall not exceed  $\pm 2\%$  over the range of interest. The WMO specification for a first class pyranometer is  $\pm 1\%$ .

**6.1.1.3 Nonlinearity of Response.** Unless the pyranometer was supplied with a calibration curve relating the output to the irradiation, its response shall not depart more than  $\pm 1\%$  from being linear over the range of irradiation existing during the tests.

**6.1.1.4 Time Response of Pyranometer and Pyrheliometer.** The time constant of the pyranometer, defined as the time required for the instrument to achieve a reading of  $(1 - 1/e) = 63.2\%$  of its final reading after a step change in irradiation, shall be less than 5 seconds. The time constant for the pyrheliometer (if used) shall be less than 25 seconds.

**6.1.1.5 Variation of Response with Angle of Incidence.** Ideally the response of the pyranometer is proportional to the cosine of the incident angle of the direct solar beam and is constant at all azimuth angles. The pyranometer's deviation from a true cosine response shall be less than  $\pm 1\%$  for the incident angles encountered during the test(s).

**6.1.1.6 Precautions for Effects of Humidity and Moisture.** The pyranometer shall be provided with a means of preventing accumulation of moisture that may condense on surfaces within the instrument and affect its reading. An instrument with a desiccator that can be inspected is required. The ambient relative humidity and condition of the desiccator should be observed prior to and following any daily measurement sequence.

**6.1.2 Calibration.** The pyranometer shall be calibrated for solar response within 12 months preceding the collector test(s) against another pyranometer whose calibration uncertainty relative to recognized measurement standards is known. Any change of more than  $\pm 1\%$  over a year period shall require the use of more frequent calibration or replacement of the instrument. If the instrument is damaged in any significant manner, it shall be recalibrated or replaced.

**6.1.3 Measurement of Direct Component of Irradiation.** When a pyrheliometer is available, it may be used to determine the direct component of the irradiation incident on a tilted pyranometer. Alternately, the diffuse component may be determined by shading the tilted pyranometer from the direct irradiation. (See Section 8.3.1 and Ref. 7). At non-horizontal attitudes, ground features which can affect readings shall be noted and their effect on calibration shall be documented.

### 6.2 Temperature Measurements.

**6.2.1 Standard Practice.** Temperature measurements shall be made in accordance with ASHRAE Standard 41.1-1986<sup>8</sup>.

**6.2.2 Accuracy and Precision.** The accuracy and precision of the instruments including their associated readout devices shall be within the limits as follows:

Instrument	Instrument
Accuracy*	Precision**
Temperature ± 0.5°C (± 0.9°F)	± 0.2°C (± 0.36°F)
Temperature ± 0.01°C (± 0.018°F)	± 0.01°C (± 0.018°F)

\*The ability of the instrument to indicate the true value of the measured quantity.

\*\*Closeness of agreement among repeated measurements of the same physical quantity.

**6.2.3 Temperature Difference Measurements Across the Solar Collector.** The temperature difference of the transfer liquid across the solar collector may be measured with one of the following<sup>8</sup>:

- a. A thermopile
- b. Calibrated resistance thermometers connected in two arms of a bridge circuit.
- c. Precision thermometers.
- d. Calibrated thermistors.
- e. Calibrated matched type-T thermocouples
- f. Quartz thermometers.

**6.2.4 Scale Divisions.** In no case should the smallest scale division of the instrument or instrument system exceed 2 times the specified precision. For example, if the specified precision is ± 0.1°C (± 0.18°F), the smallest scale division should not exceed 0.2°C (0.36°F).

**6.2.5 Instrumentation.** The instruments shall be configured and used in accordance with Section 7 of this Standard.

**6.3 Dew Point Temperature.** The dew point temperature of the ambient air shall be measured for each data point to an accuracy of ± 1°C (± 1.8°F).

**6.4 Liquid Flow Measurements.** The accuracy of the liquid flow rate measurement shall be equal to or better than ± 1.0% of the measured value in mass units per unit time.

## 6.5 Integrators and Recorders.

**6.5.1 Strip Chart Recorders.** Strip chart recorders used shall have an accuracy equal to or better than ± 0.5% of the full scale reading and have a time constant of 1 second or less. The peak signal indication shall be between 50 and 100% of full scale.

**6.5.2 Electronic Integrators.** Electronic integrators used shall have an accuracy equal to or better than ± 1.0% of the measured value.

**6.5.3 Input Impedance.** The input impedance of the recorders shall be greater than 1000 times the impedance of the sensor.

**6.6 Time and Mass Measurements.** For calibration purposes, time measurements and mass measurements shall be made to an accuracy of ± 0.20%<sup>9</sup>.

**6.7 Wind Speed.** The wind speed shall be measured with an instrument and associated readout device that can determine the integrated average wind speed for each data point to an accuracy of ± 0.2 m/s (± 0.5 mph).

**6.8 Pressure Drop Across Collector.** The static pressure drop across the solar collector shall be measured with an instrument having an accuracy of ± 5.0 Pa (± 0.2 in. of water).

## 7.0 APPARATUS AND METHOD OF TESTING

**7.1 Test Configuration.** The test configurations for testing solar collectors are shown in Figs. 1, 2, and 3 and are representative rather than exact. They are not drawn to scale. Whichever configuration is used, the test conditions specified herein must be satisfied. When the circulating transfer liquid is susceptible to evaporation losses as in Fig. 2, care should be taken to minimize and to account for the evaporation losses.

**7.1.1 Solar Collector.** The solar collector shall be rigidly mounted to the test rack at the predetermined tilt angle with backing determined in accordance with the provisions of Section 5.1.3. It is essential that the test rack, whether fixed or movable, be unaffected by strong gusts of wind.

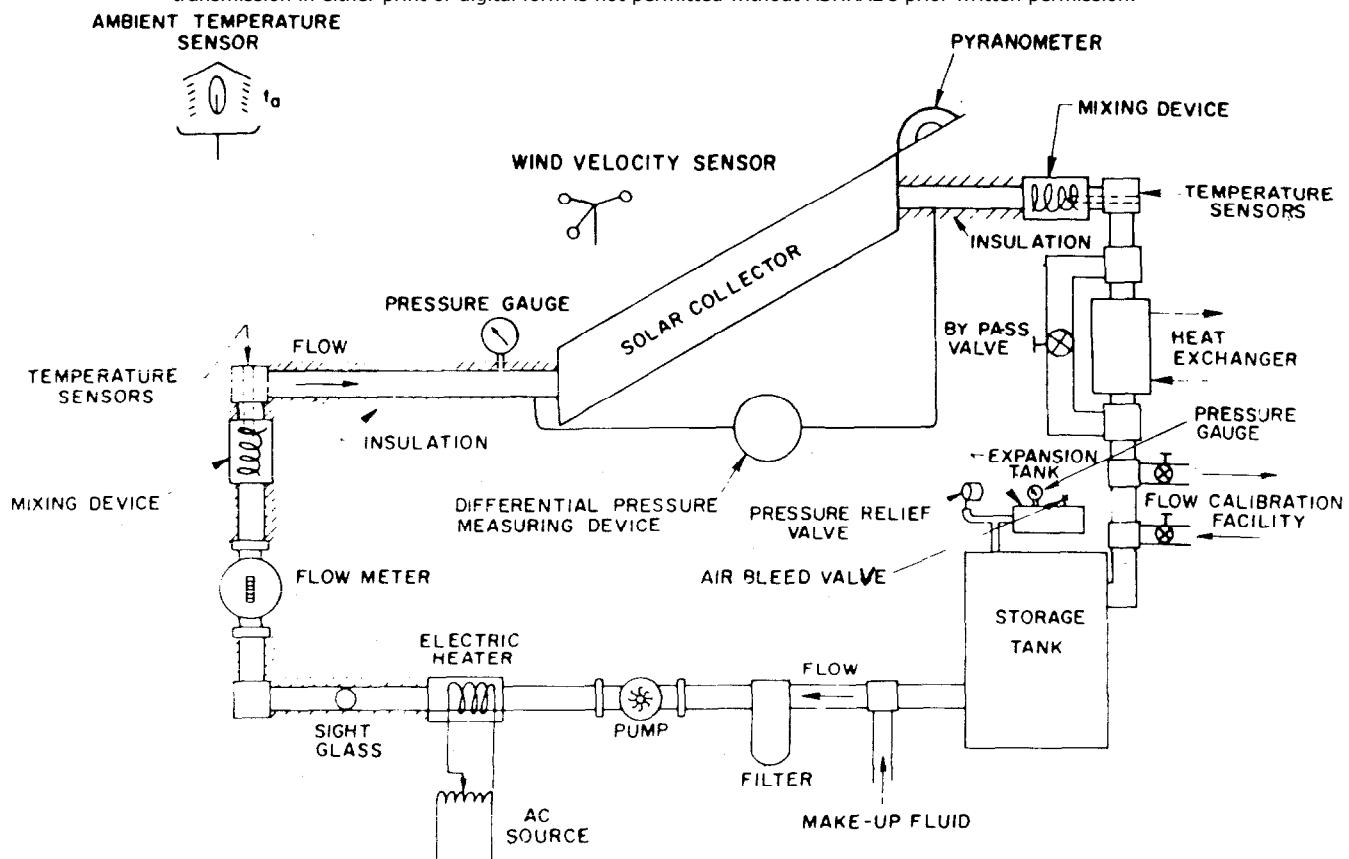
**7.1.2 Ambient Temperature.** The ambient temperature sensors shall be housed in a well-ventilated instrumentation shelter with its bottom 1.25 m (4.1 ft) above the ground and with its door facing north, so that the sun's direct beam cannot fall upon the sensors when the door is opened. The instrument shelter shall be painted white outside and shall not be closer to any obstruction than twice the height of the obstruction itself (i.e., trees, fences, buildings, etc.).<sup>10</sup>

**7.1.3 Solar Radiation.** Irradiation measurements shall be reported in terms of apparent solar time for the test site (see Appendix B).

A pyranometer for measuring the total radiation and a suitable method for determining the direct component shall be utilized for all collector tests. The pyranometer shall meet the requirements specified in 6.1.1 and shall be mounted such that its sensor is coplanar with the plane of the collector aperture. It shall not cast a shadow onto the collector aperture at any time during the test period. The pyranometer shall not be mounted so as to receive a percentage of terrestrial radiation that is disproportionate with that received by the collector. It is recommended that the pyranometer be mounted near the upper-half periphery of the collector, and in the upper center of the collector array. The pyranometer should be oriented so that the emerging leads of the connector are located north of the receiving surface (in the Northern Hemisphere), or are otherwise shaded to minimize solar heating of the electrical connections.

Care should also be taken to minimize reflected and reradiated energy from the solar collector onto the pyranometer. Some pyranometers are supplied with shields. Pyranometers not supplied with a shield may be susceptible to error due to reflections by radiation that originates below the plane of the sensor.

The direct and diffuse components of the solar radiation shall be determined for each data point. This measurement can be made utilizing the shading band or shading



**Figure 1. Closed-Loop Testing Configuration for the Solar Collector**

disc method using a pyranometer (see 8.3.1) or by using a pyrheliometer.

**7.1.4 Temperature Difference Measurements Across the Solar Collector.** The temperature difference of the transfer liquid between entering and leaving the solar collector shall be measured in accordance with 6.2.2 and 6.2.3.

To minimize temperature measurement error, each probe shall be located as close as possible to the inlet or outlet of the solar collector and shall be inserted into a mixing device located as shown in Figs. 1, 2, and 3. In addition, the inlet and outlet piping between the mixing devices and the collector shall be insulated in such a manner that the calculated heat loss or gain from the ambient air will not cause a temperature change for any test of more than  $0.01^{\circ}\text{C}$  ( $0.018^{\circ}\text{F}$ ) between each mixing device and the collector. Both inlet and outlet piping shall be treated in like manner.

**7.1.5 Additional Temperature Measurements.** The temperature of the transfer liquid at each of the two positions cited above shall be measured by inserting appropriate sensors into the mixing devices (except for the case where precision thermometers are employed to determine temperature difference). Reference 8 should be followed in making these measurements.

**7.1.6 Pressure Drop Across the Solar Collector.** The pressure drop across the solar collector shall be measured using static pressure tap holes and an instrument such as a manometer or a differential pressure transducer. The edges of the holes on the inside surface of the pipe should be free of burrs. The holes should be as small as practical

and should not exceed  $1.6\text{ mm}$  ( $1/16\text{ in.}$ ) in diameter. The thickness of the pipe wall should be at least 2.5 times the hole diameter. Provisions shall be made for determining the absolute pressure of the entering transfer liquid<sup>11</sup>. If the cross-sectional areas at the two sensing locations of the differential pressure measuring device are unequal, a correction for the difference in velocity pressure at the two locations shall be made.

**7.1.7 Reconditioning Apparatus.** As shown in Figure 1, the use of a closed-loop test facility requires that a heat exchanger be employed to cool the transfer liquid and an adjustable in-line electrical resistance heater be used to control the inlet temperature to the prescribed test values. This combination of equipment or its equivalent shall control the temperature of the liquid entering the collector to within  $\pm 0.1^{\circ}\text{C}$  ( $\pm 0.18^{\circ}\text{F}$ ) for each data point.

A heat exchanger is also recommended when employing an open-loop test facility similar to Fig. 2 to cool the outlet liquid to minimize evaporation losses and thus minimize weighing errors in the gravimetric determination of mass flow rate. Figure 3 shows an open-loop system in which the liquid is not recirculated.

**7.1.8 Additional Equipment.** A pump and a means of adjusting the flow rate of the transfer liquid shall be provided at the relative locations shown in Figs. 1, 2, and 3. Depending upon the test apparatus design, an additional throttle valve may be required in the line just preceding the solar collector for proper control.

A storage tank, expansion tank, air vent, and a pressure relief valve should be installed in the closed-loop test con-

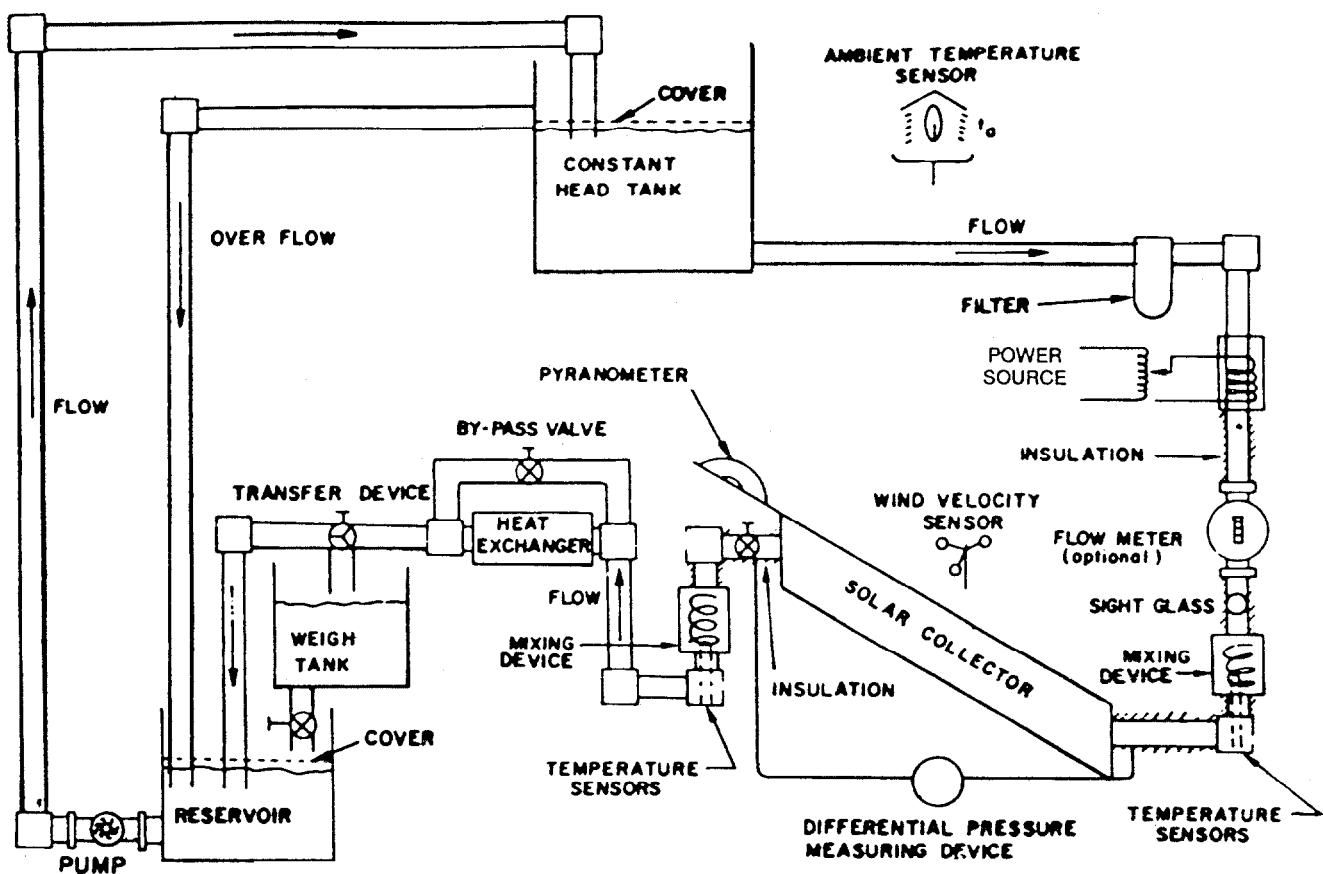


Figure 2. Open-Loop Testing Configuration for the Solar Collector

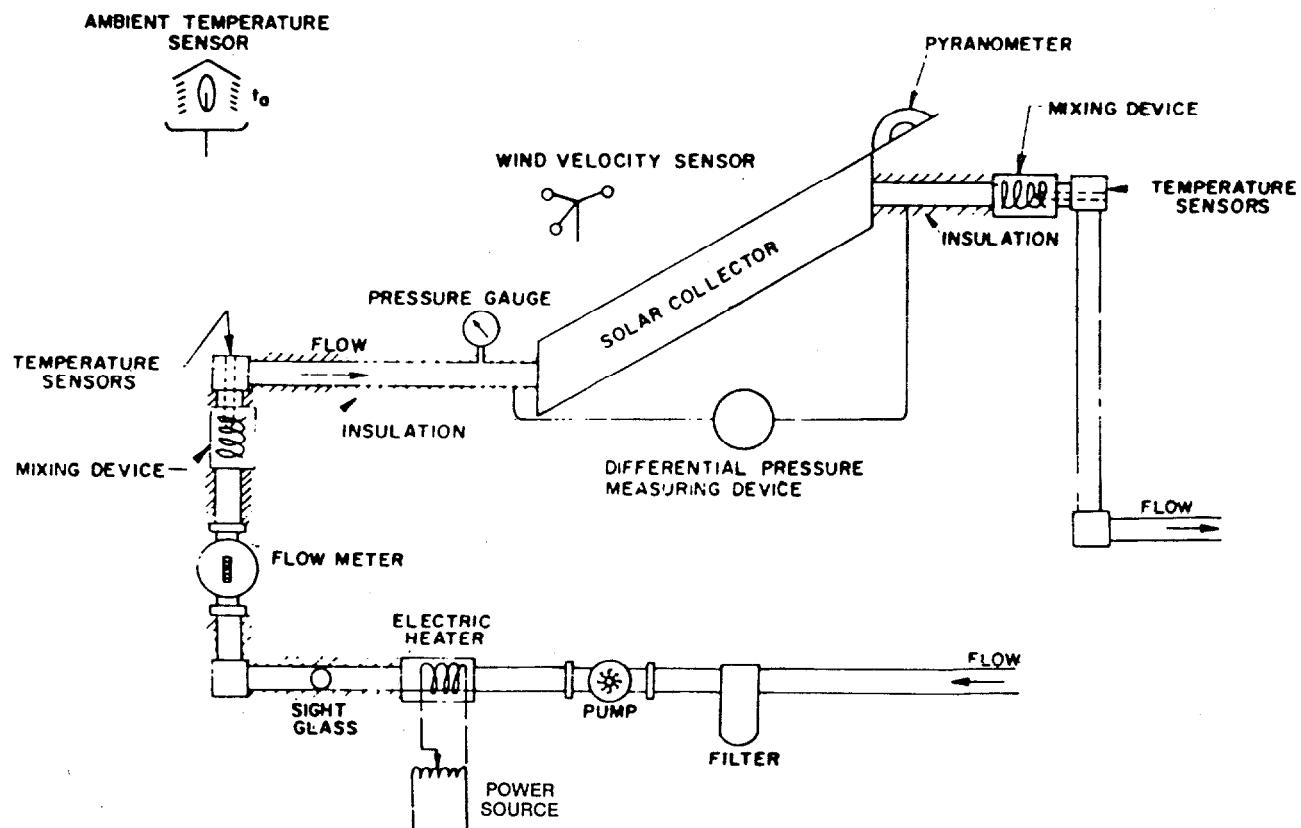


Figure 3. Open-Loop Testing Configuration for the Solar Collector for Use when Liquid is Supplied Continuously

figuration as shown in Fig. 1 to stabilize the flow and allow the transfer liquid to expand and contract freely in the system. Figure 1 should not be interpreted to mean that the relief valve and expansion tank must necessarily be located below the collector. Depending upon the design, an expansion tank and relief valve are sometimes inserted between the pump and the collector in an open-loop test facility.

Filters and a sight glass should be installed within the apparatus to ensure that the transfer liquid passing through the collector is free of contaminants, including air bubbles.

**7.2 Indoor Testing With a Solar Simulator.** A solar simulator may be used in lieu of outdoor testing to determine the steady-state thermal performance of the solar collectors under controlled conditions of wind and ambient temperature. References 12, 13, and 14 describe typical simulators used for testing collectors. Solar simulators employed in the testing procedure shall have the following characteristics:

**7.2.1 Spectral Qualities.** The simulator shall duplicate the spectrum of average North American sunlight as closely as possible. This average is best represented by an air mass 2 solar spectrum.<sup>12</sup> The measured energy spectrum shall not deviate from the air mass 2 spectrum more than specified in the following table:

Band $\lambda \mu\text{m}$	Air Mass 2, Percent of Energy in Band	Maximum Deviation of Simulator
0.3-0.4	2.7	15%
0.4-0.7	44.4	9
0.7-1.0	28.6	3
1.0- $\infty$	24.3	10

In addition, the calculated solar absorptance,  $\alpha$ , of the spectrally selective surface described in Ref. 15 irradiated by the simulator shall not differ more than 1% from the value measured under air mass 2 sunlight.

There shall not be a significant change in the simulator's energy spectrum for variations in power output. The calculated solar absorptance of the above specific selective surface 15 irradiated by the simulator shall not change by more than 1% for a change in radiation flux from 0.45 to 0.75 of one Solar Constant.\*

**7.2.2 Uniformity.** The departure from uniformity of the illumination of the solar simulator beam over the test plane (the plane of the collector aperture) shall be such that the high and low irradiation values of the illuminated plane shall not exceed  $\pm 10\%$  of the average irradiation.

**7.2.3 Collimation.** The collimation shall be such that 95% of the energy output of the simulator is within a subtended angle of less than 12 degrees.

**7.2.4 Simulator-to-Collector Configuration Factor.** The collector configuration factor\*\* between the solar simulator and the solar collector shall not exceed 0.05.

**7.2.5 Air Flow Across Collector.** A fan shall be provided to cause a substantially uniform air flow across the

\* 1353 W/m<sup>2</sup> [429.2 Btu/(h · ft<sup>2</sup>)].<sup>16</sup>

\*\* Configuration factor, radiation exchange factor, or radiation shape factor are defined in most heat transfer textbooks, for example, Ref. 17.

collector surface at a wind speed not in excess of 1.3 m/s (3.0 mph).

## 8.0 TEST PROCEDURES AND COMPUTATIONS

**8.1 General.** The thermal performance of unglazed flat-plate liquid-type collectors is determined in part by obtaining values of instantaneous efficiency for a combination of values of incident radiation and ambient temperature, while inlet liquid temperature is both above and below ambient. This requires experimentally measuring the rate of incident solar radiation onto the solar collector as well as the rate of energy addition to the transfer liquid as it passes through the collector, all under steady-state or quasi-steady-state conditions. In addition, tests are performed to determine how the steady-state thermal efficiency varies with the incident angle between the direct solar beam and the collector.

### 8.2 Basic Performance Equations.

**8.2.1 Collector Thermal Efficiency.** It has been shown and discussed by a number of investigators<sup>18-21</sup> that the performance of a flat-plate solar collector operating under steady-state conditions can be successfully described by the following relationship:

$$\frac{q_u}{A_a} = I_i(\tau\alpha)_c - U_L(t_p - t_a) \\ = \frac{\dot{m}}{A_a} c_p(t_{f,e} - t_{f,i}) \quad (8.1)$$

To assist in obtaining detailed information about the performance of flat-plate collectors and to preclude the necessity for determining the average temperature of the absorber surface, it has been convenient to introduce a parameter  $F_R$  where:

$$F_R = \frac{\text{actual useful energy collector by a flat-plate collector}}{\text{useful energy collector if the entire flat-plate collector surface were at the inlet fluid temperature}}$$

Introducing this factor into Equation (8.1) results in

$$\frac{q_u}{A_a} = F_R [I_i(\tau\alpha)_c - U_L(t_{f,i} - t_a)] \\ = \frac{\dot{m}}{A_a} c_p(t_{f,e} - t_{f,i}) \quad (8.2)$$

If the solar collector efficiency is defined as

$$n_g = \frac{\text{actual useful energy collected}}{\text{solar energy incident upon or} \\ \text{intercepted by the collector}} = \frac{q_u/A_g}{I_i} \quad (8.3)$$

then the efficiency of the flat-plate collector is given by:

$$n_g = (A_a/A_g) F_R [(\tau\alpha)_c - U_L \frac{(t_{f,i} - t_a)}{I_i}] \\ = \frac{\dot{m} c_p (t_{f,e} - t_{f,i})}{A_g I_i} \quad (8.4)$$

$t_{f,i}$  and  $t_{f,e}$  may be either greater or less than  $t_a$  for collectors used in low temperature applications.

Equation (8.4) indicates that if the efficiency,  $n_g$ , is plotted against  $(t_{f,i} - t_a)/I_i$ , a straight line will result where the slope is equal to  $(A_a/A_g) F_R U_L$  and the y intercept is equal to  $(A_a/A_g) F_R (\tau\alpha)_c$ . In reality,  $U_L$  is not a constant but rather a function of the temperature of the

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collector and often in contradiction to the condition of adiabatic collector surface. In addition, the product  $(\tau\alpha)$  varies with the incident angle between the solar beam and the collector. However, in the range of values of parameter  $(t_{f,i} - t_a)/I_t$  of interest in low temperature applications,  $-0.020$  to  $+0.030$  ( $^{\circ}\text{C} \cdot \text{m}^2/\text{W}$ ),  $(A_a/A_g)F_R U_L$  is essentially constant and the efficiency plot will be nearly a straight line within that range.

The procedures outlined in this document are intended to control the test conditions so that a well defined efficiency curve can be obtained with a minimum of scatter. Figure 4 shows a typical result of tests conducted under near-normal-incidence conditions on an unglazed collector.

Although a straight-line representation of the efficiency curve will suffice for almost all low temperature applications, some collectors may require the use of a higher order fit, i.e., a second order polynomial, due to variation of  $U_L$  with collector temperature.

**8.2.2 Collector Incident Angle Modifier.** The effective transmittance absorptance factor,  $(\tau\alpha)_e$ , can be replaced in the general equations (8.1), (8.2), and (8.4) by the value at normal incidence,  $(\tau\alpha)_{e,n}$ ,  $K_{\alpha\tau}$ , is introduced.<sup>22</sup> Equation (8.4) then becomes:

$$\eta_g = (A_a/A_g)F_R [K_{\alpha\tau}(\tau\alpha)_{e,n} - U_L \frac{(t_{f,i} - t_a)}{I_t}] + \frac{mc_p}{a_g I_t} (t_{f,e} - t_{f,i}) \quad (8.5)$$

In terms of one constant, the incident angle modifier  $K_{\alpha\tau}$  provides a more convenient way to represent the performance of solar collectors,  $(\tau\alpha)_e$  should vary with incident angle according to the general expression:

$$(\tau\alpha)_e = a - (b/\cos\Phi) \quad (8.6)$$

Comparing equations (8.5) and (8.6)

$$K_{\alpha\tau}(\tau\alpha)_{e,n} = a - \frac{b}{\cos\Phi} \quad (8.7)$$

Solving the equation for  $K_{\alpha\tau}$  and recognizing that  $(\tau\alpha)_{e,n} = a - b$ ;

$$K_{\alpha\tau} = 1 - \frac{b}{a-b} \left( \frac{1}{\cos\Phi} - 1 \right) \quad (8.8)$$

In terms of one constant, the incident angle modifier  $K_{\alpha\tau}$  is:

$$K_{\alpha\tau} = 1 - b_o \left( \frac{1}{\cos\Phi} - 1 \right) \quad (8.9)$$

Figure 5 shows the variation of  $K_{\alpha\tau}$  with incident angle for a typical unglazed collector.

The significance of the incident angle modifier to the test procedures outlined herein is that the thermal efficiency values are determined for the collector at or near normal incidence conditions. Therefore, the y intercept of the efficiency curve is equal to  $(A_a/A_g)F_R (\tau\alpha)_{e,n}$ . A separate test is conducted to determine the value of  $b_o$  and hence  $K_{\alpha\tau}$  so that the performance of the collector can be predicted

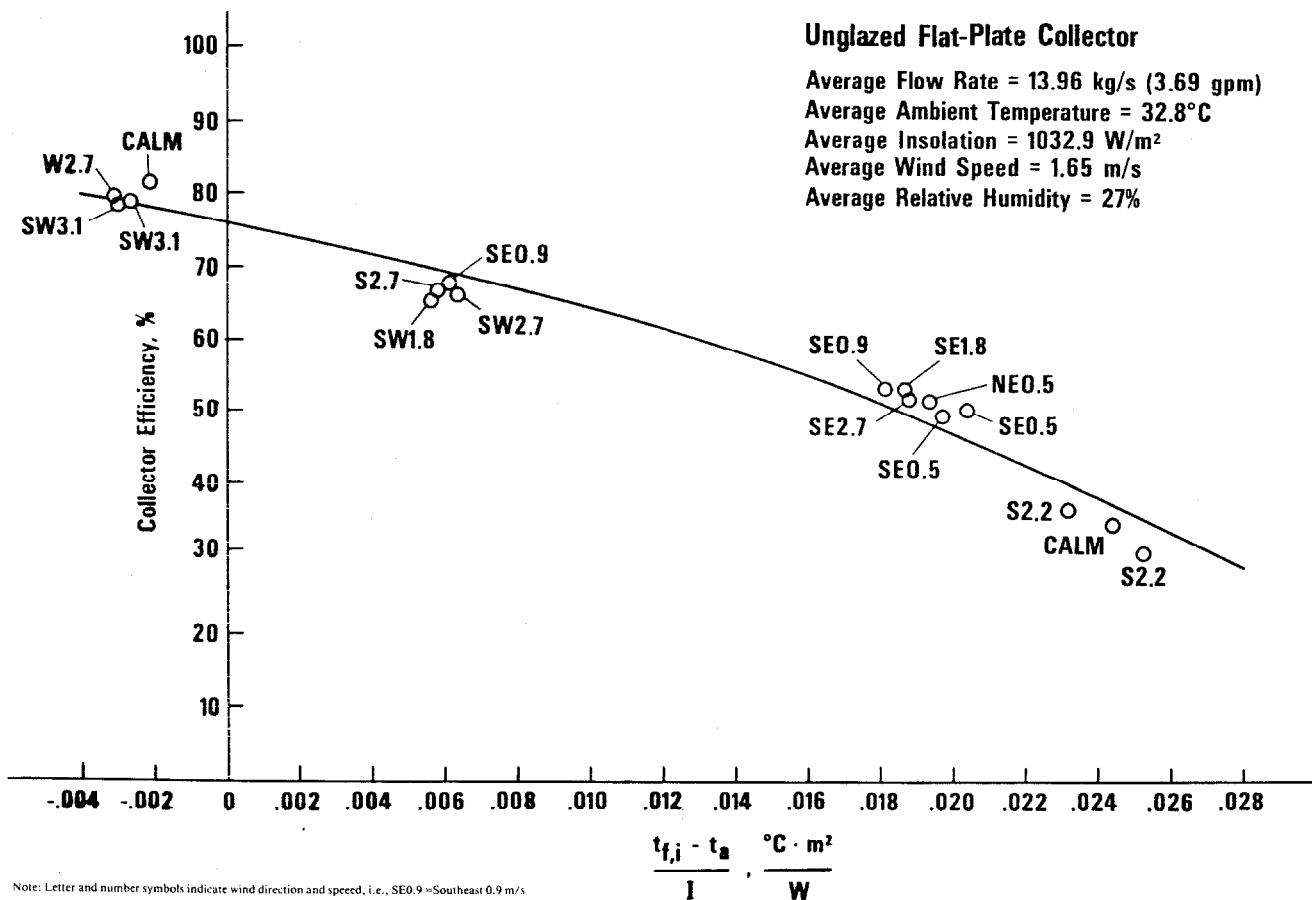


Figure 4. Hottel-Whillier-Newton Plot of Thermal Efficiency for an Unglazed Flat-Plate Liquid-Type Solar Collector Using Water as the Transfer Liquid

under a wide range of conditions and/or time of day using Equation (8.5).

It is recognized that some collector designs require tests in two different incident angle planes to account for non-symmetrical response to irradiation as solar azimuth and altitude change throughout the day. In such cases, both incident angle modifiers should be determined in the different planes.

**8.3 Test Procedure.** The first performance tests to be conducted are a series of thermal efficiency tests as explained in 8.3.1. The value of the collector incident angle modifier is then determined in accordance with 8.3.2. The incident angle modifier test is not required for those collectors for which the angular response characteristics are known.

#### 8.3.1 Experimental Determination of the Collector

**Thermal Efficiency.** The testing of the solar collector to determine its thermal efficiency shall be conducted in such a way that a governing efficiency curve for near-normal-incidence is determined under test conditions described in Section 5 and this section. At least four different values of inlet liquid temperature shall be used to obtain the values of  $\Delta t/I_i$ . At least one value of  $\Delta t/I_i$  shall be in the negative range of approximately  $-0.02$  to  $-0.15^\circ (\text{C} \cdot \text{m}^2)/\text{W}$ . The remaining values shall be in the positive range of  $+0.01$  to  $+0.030 (\text{C} \cdot \text{m}^2)/\text{W}$ .

At least four data points shall be taken for each value of

$t_{f,i}$ ; two during the time period preceding solar noon and two in the period following solar noon, the specific periods being chosen so that the data points represent times symmetrical to solar noon. This latter requirement is made so that any "transient effects" that may be present will not bias the test results when they are used for design purposes. The requirement for obtaining data points equally divided between morning and afternoon does not apply when testing with an altazimuth mount. All test data shall be reported in addition to the fitted curve (see Section 9) so that any difference in efficiency due solely to the operating temperature level of the collector can be discerned in the test report. The curve shall be established by data points that represent efficiency values determined by integrating over five minutes. The integrated value of incident solar radiation will be divided into the integrated value of energy obtained from the collector to obtain the efficiency value for that test period.

When an indoor solar simulator is employed and true steady-state conditions can be obtained, the time interval specified above is not applicable. In this case, data may be considered as steady-state when the collector outlet temperature does not change (within the limits of measurement) in a five minute time period. Instantaneous data may then be used to determine instantaneous efficiency.

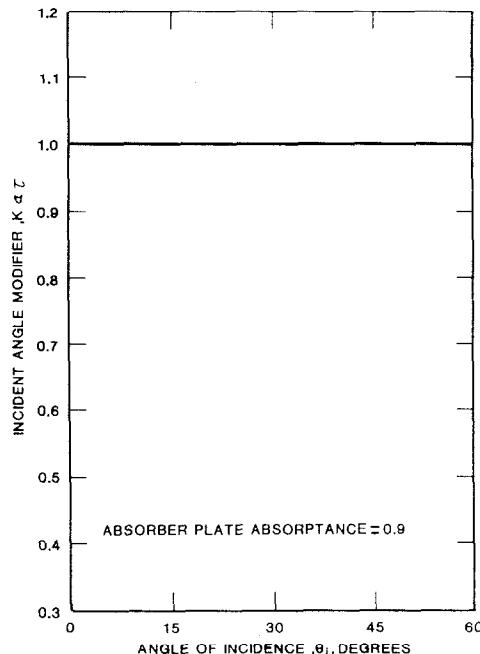
In conducting outdoor tests, care should be taken to ensure that the incident solar energy is steady for each time interval during which an efficiency value is calculated. Either electronic integrators or continuous pen strip chart recorders may be used to determine the integrated values of incident solar radiation and temperature rise across the collector. However a strip chart recorder with a recommended chart speed of  $30 \text{ cm/h}$  ( $12 \text{ in./h}$ ) or greater must always be used to monitor the output of the pyranometer to ensure that the incident radiation has remained steady during the test period. Figures 6 and 7 show strip chart recordings of incident solar radiation on a horizontal surface. Whereas the conditions of Fig. 6 would be perfectly acceptable for obtaining efficiency values, those of Fig. 7 would not be\*.

The surface of the exposed envelopes of the pyranometer(s) and pyrheliometer (if used) should be wiped clean and dry prior to the tests. If local pollution or sand has formed a deposit on the transparent surfaces, the wiping should be carried out very gently preferably after blowing off most of the loose material or after wetting it a little, in order to prevent scratching of the surface. This is particularly important since such abrasive action can appreciably alter the original transmission properties of the enclosing envelope.

The pyranometer(s) shall be checked prior to testing to see if there is any accumulation of water vapor enclosed within the glass cover. The use of wet pyranometers (where moisture is visible) shall not be allowed.

In order to obtain sufficiently good steady-state or quasi-steady-state conditions for the solar collection process, the transfer, liquid should be circulated through the collector

\* One or two "blips" of  $10 \text{ s}$  or less occurring the test period such as at 12.18 in Figure 6 are acceptable.



**Figure 5. Example of Incident Angle Modifier for an Unglazed Flat-Plate Solar Collector with a Non-Selective Surface**

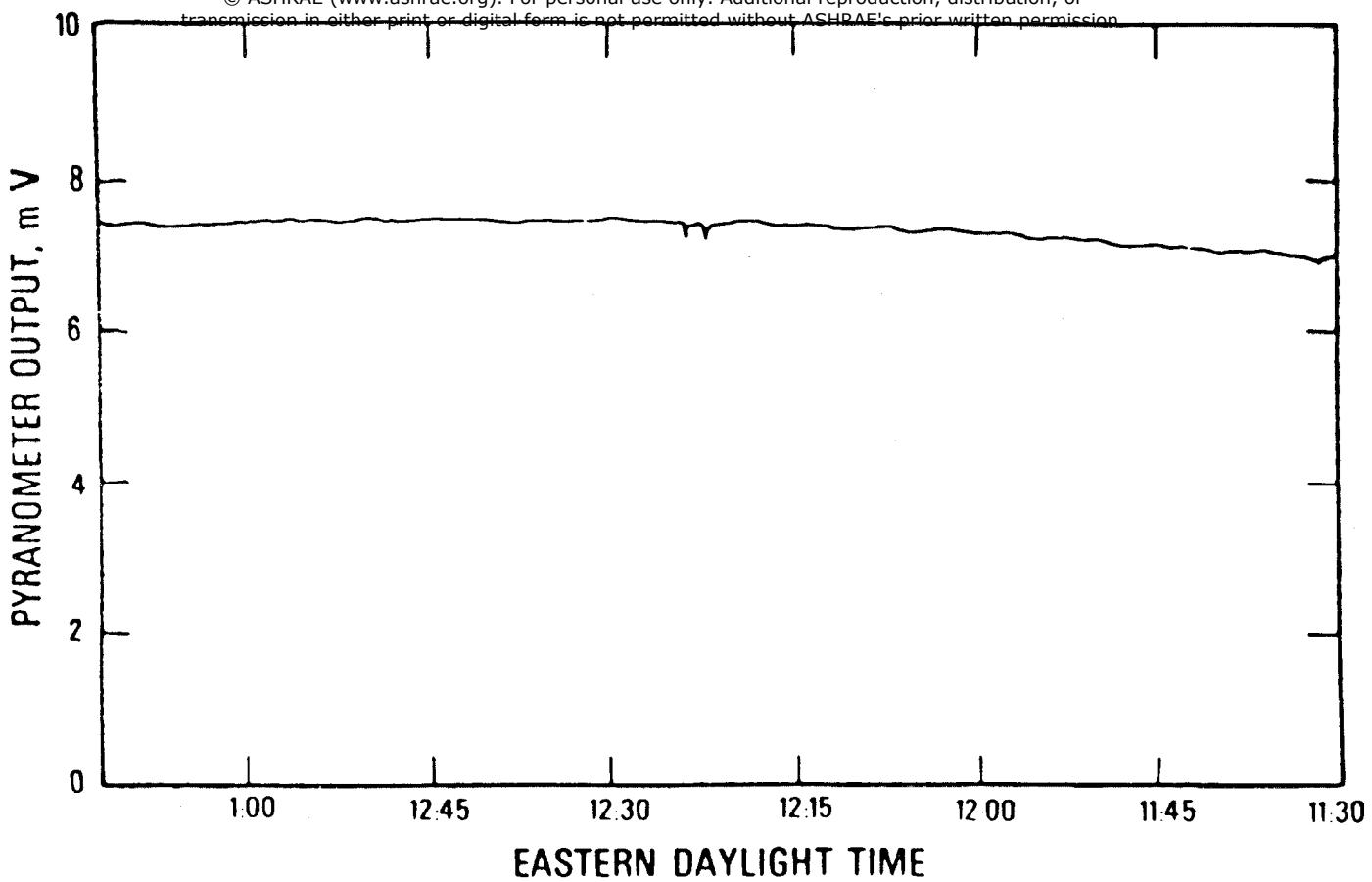


Figure 6. Incident Solar Radiation on a Horizontal Surface in Gaithersburg, Md, March 13, 1974.

at the appropriate inlet temperature level until the temperature has remained constant for 15 min prior to the period in which data will be taken to calculate the efficiency values.

When using an indoor simulator, the following starting procedure has been found satisfactory. The transfer liquid is circulated through the collector at the inlet temperature chosen for the test. After equilibrium is established for the chosen inlet temperature, the simulator is turned on and the desired radiant flux obtained by adjusting the lamp voltage. A check should be made to ensure that the flow rate of the transfer liquid does not vary by more than  $\pm 1\%$  and that the incident radiation is steady as described above.

The flow rate of heat transfer liquid through the collector shall be standardized for all data points. The recommended value of flow rate per unit area (transparent frontal or aperture) for standard tests is  $0.07 \text{ kg/s} \cdot \text{m}^2$  ( $51.5 \text{ lb}/(\text{h} \cdot \text{ft}^2)$ ). It is recognized that in some cases the manufacturer of a collector will recommend a design flow rate different from that specified above. In such cases the recommended design flow rate should be used.

The fraction of the incident solar radiation which is diffuse must be determined and reported for each efficiency data point. In the absence of a normal incidence pyrheliometer, two pyranometers may be used, one of which uses a shading band<sup>7</sup> or if only a single pyranometer is used, its sensing element shall be shaded from the direct beam of sun just prior to and just following each test for a short period and the value of the incident diffuse radiation determined. This shall be accomplished by using a small disc attached to a slender rod held in a direct line between the pyranom-

eter and the sun. The disc should be just large enough to shade the sensing element alone. As an example, see [5].

The steady wind speed across the collector as measured per 5.1.7 and 6.7 shall be less than  $1.3 \text{ m/s}$  (3.0 mph). Average wind speed shall be recorded for each data point on the efficiency curve.

**8.3.2 Experimental Determination of Collector Incident Angle Modifier for Stationary Collectors.** The testing of the solar collector to determine its incident angle modifier can be done by either of two methods.

**Method (1):** This method is applicable for testing indoors using a solar simulator or outdoors using a movable test rack so that the orientation of the collector can be arbitrarily adjusted with respect to the direction of the direct solar beam. Four separate efficiency values are determined in general accordance with the method described in 8.3.1. For each data point, the inlet temperature of the transfer liquid is controlled as close as possible to within  $\pm 1^\circ\text{C}$  ( $\pm 1.8^\circ\text{F}$ ) of the ambient air temperature. The collector is oriented so that the average incident angles between it and the direct solar beam for the four test conditions are respectively, approximately 0, 30, 45 and 60 degrees  $\pm 3^\circ$ . The foregoing values are appropriate for most unglazed collectors.

**Method (2):** This method is applicable for testing outside using a permanent test rack where the collector orientation cannot be arbitrarily adjusted with respect to the direction of the incident solar radiation (except for adjustments in tilt). Six separate efficiency values are determined in general accordance with the method described in 8.3.1. For each data point the inlet temperature of the transfer liquid is

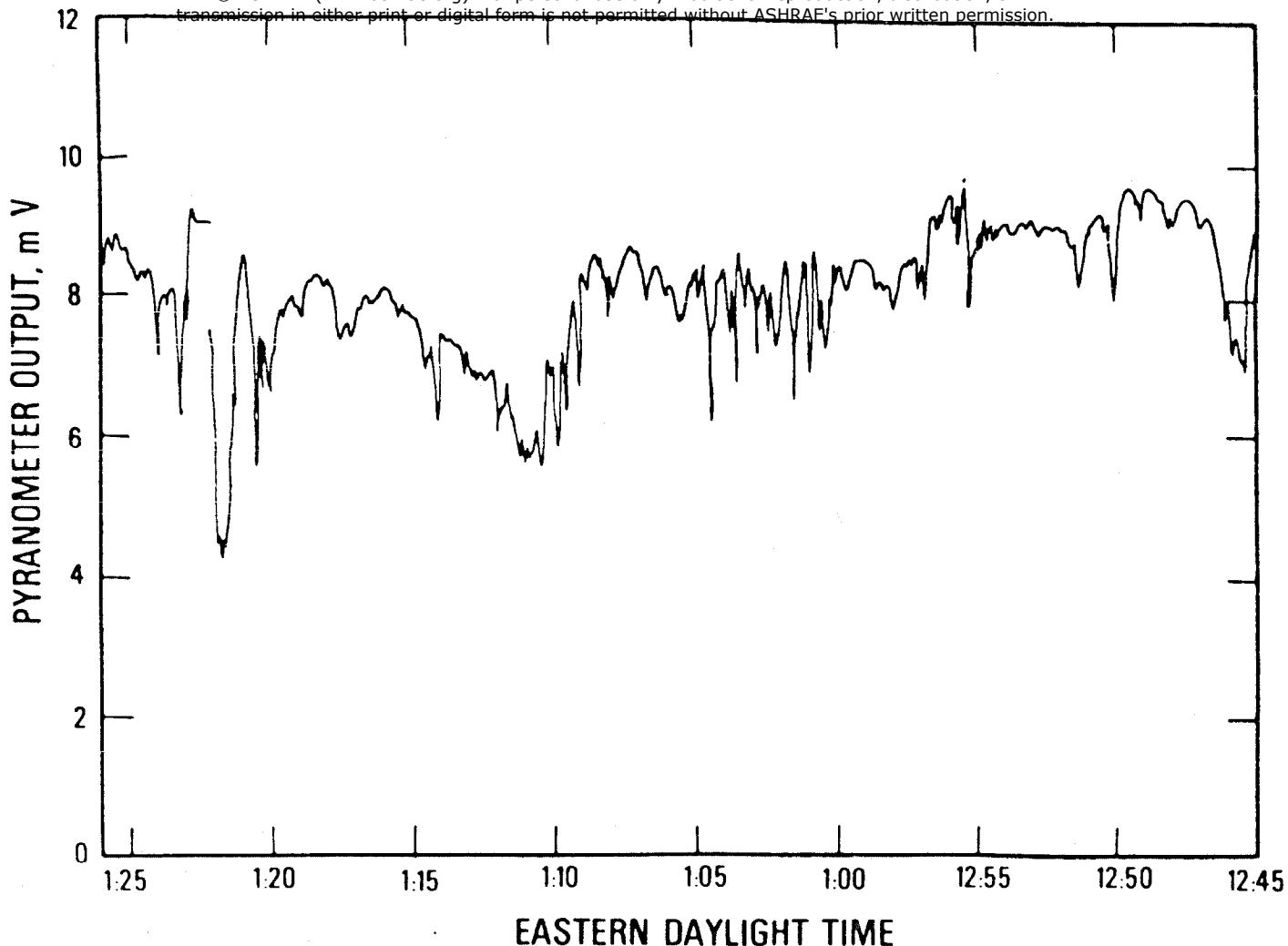


Figure 7. Incident Solar Radiation on a Horizontal Surface in Gaithersburg, Md, March 11, 1974

controlled as close as possible to within  $\pm 1^\circ\text{C}$  ( $\pm 1.8^\circ\text{F}$ ) of the ambient air temperature. The efficiency values are determined in three pairs where each pair includes a value of efficiency early in the day and a second value late in the day. The average incident angle between the collector and the direct solar beam for both data points is the same. The efficiency of the collector for the specific incident angle shall be considered equal to the average of the two values. As with Method (I), data should be collected for average incident angles of 0, 30, 45 and 60 degrees,  $\pm 3^\circ$ .

**8.4 Computation of Collector Thermal Efficiency.** For the test interval for each efficiency data point, the efficiency value is calculated using the equation:

$$\eta_g = \frac{\dot{m} c_p \int_{T_1}^{T_2} (t_{f,e} - t_{f,i}) dT}{A_g \int_{T_1}^{T_2} I_t dT} \quad (8.10)$$

The quantities  $\dot{m}$  and  $c_p$  have been taken out of the integration in the numerator since they remain essentially constant during the test. Note that the collector area used for the calculation is not the absorbing surface area but rather the gross collector area.

At least sixteen data points shall be obtained for the establishment of each efficiency curve and an equation for the curve shall be obtained using the standard technique of

a least-square fit.\* In most cases, a linear or second order fit will suffice. The curve should not be extrapolated beyond the limits of data.

**8.5 Computation of Collector Incident Angle Modifier.** Regardless of which experimental method in Section 8.3.2 is used, three different values of the thermal efficiency of the collector shall be determined corresponding to three different values of incident angle. Since the inlet collector temperature is held sufficiently close to the ambient air temperature,  $(t_{f,i} - t_a) \sim 0$ , the relationship between  $K_{\alpha\tau}$  and the efficiency, according to Equation (8.5), is:

$$K_{\alpha\tau} = \frac{\eta_g}{(A_a/A_g) F_R(\tau\alpha)_{c,n}} \quad (8.11)$$

Since  $(A_a/A_g) F_R(\tau\alpha)_{c,n}$  will have already been obtained as the intercept of the efficiency curve determined in accordance with Sections 8.3.1 and 8.4, three different values of  $K_{\alpha\tau}$  can be computed for the different incident angles using Equation (8.11). The value of  $b_o$  may be determined using Equation (8.9) and the standard technique of a least-squares fit to a first-order polynomial. Other methods of correlation may be used to describe an equation for the incident angle modifier.

\* One should consult any standard text discussing analysis of experimental data for presentation of this technique (e.g. Refs. 23 and 24).

If the inlet liquid temperature cannot be controlled to equal the ambient air temperature [within  $\pm 1.0^\circ\text{C}$  ( $\pm 1.8^\circ\text{F}$ )], an estimate of the  $(A_a/A_g)F_R U_L$  product should be made for the collector for the conditions of the test and each value of  $K_{\alpha\tau}$  computed as:

$$K_{\alpha\tau} = \frac{\eta_g + (A_a/A_g)F_R U_L(t_{f,i} - t_a)/I}{(A_a/A_g)F_R(\tau\alpha)_{c,n}} \quad (8.12)$$

Alternatively, each data point can be plotted on the same plot with the efficiency curve determined in accordance with 8.3.1 and 8.4 and a curve drawn through each point parallel to the efficiency curve and made to intersect the y axis. The values of the y intercept are the efficiency values that would have resulted had the inlet liquid temperature been controlled to equal the ambient air temperature.

Therefore, those values can be used in conjunction with equation (8.11) to compute the different values of  $K_{\alpha\tau}$ .

**8.6 Computation of Theoretical Power Requirements.** In order to calculate theoretical power required to move the transfer liquid through the solar collector, the following equation shall be used.

$$P_{th} = \dot{m} \cdot \Delta p/w \quad (8.13)$$

## 9.0 DATA TO BE RECORDED AND TEST REPORT

**9.1 Test Data.** Table 1 lists the measurements which are to be made at the beginning of the testing day and during the individual tests to obtain an efficiency data point.

**9.2 Test Report.** Table 2 specifies the data and information that shall be reported in testing the solar collector.

**Table 1 Measurements to be Made and Test Data and Information to be Recorded**

Data	
Observer(s)	
Equipment name plate data	
Collector tilt angle, deg.	
Collector azimuth angle, deg. from South	
Collector aperture area or frontal acceptance area, $\text{m}^2$ ( $\text{ft}^2$ )	
Gross collector area, $\text{m}^2$ ( $\text{ft}^2$ )	
Local Standard Time at the beginning of the collector warm-up and at the beginning and end of each test period	
Apparent solar time, as required above	
Ambient air temperature at the beginning and end of each test period, $^\circ\text{C}$ ( $^\circ\text{F}$ )	
$\Delta t = t_{f,e} - t_{f,i}$ across solar collector (either as a continuous function of time or as a data point integrated quantity), $^\circ\text{C}$ ( $^\circ\text{F}$ )	
Inlet temperature, $t_{f,i}$ , $^\circ\text{C}$ ( $^\circ\text{F}$ )	
Outlet temperature $t_{f,e}$ , $^\circ\text{C}$ ( $^\circ\text{F}$ )	
Liquid flow rate, $\text{kg}/\text{s}$ ( $\text{lb}/\text{h}$ )	
Pressure drop across solar collector, $\text{Pa}$ ( $\text{lb}/\text{in.}^2$ )	
Height of collector outlet above the collector inlet, $\text{m}$ ( $\text{ft}$ )	
Wind speed near the collector surface or aperture (data point average), $\text{m}/\text{s}$ ( $\text{mph}$ )	
$I_t$ , the incident total solar irradiation onto the collector (as a continuous function of time, and as a data point integrated quantity if desired), $\text{W}/\text{m}^2$ ( $\text{Btu}/(\text{h} \cdot \text{ft}^2)$ ) or $\text{J}/\text{m}^2$ ( $\text{Btu}/\text{ft}^2$ )	
$I_{DN}$ , direct beam component of solar irradiation onto the collector (as a continuous function of time and as a data point integrated quantity if measured) $\text{W}/\text{m}^2$ ( $\text{Btu}/(\text{h} \cdot \text{ft}^2)$ ) or $\text{J}/\text{m}^2$ ( $\text{Btu}/\text{ft}^2$ )	
or	
$I_d$ , the diffuse component of the solar irradiation onto the collector (at the beginning of the test period and after the completion of the test period) $\text{W}/\text{m}^2$ ( $\text{Btu}/(\text{h} \cdot \text{ft}^2)$ ) or $\text{J}/\text{m}^2$ ( $\text{Btu}/\text{ft}^2$ )	
$\Phi$ , incident angle (at the beginning of each test period), deg.	
Dew-point temperature, $^\circ\text{C}$ ( $^\circ\text{F}$ )	

**Table 2 Data and Information to be Reported**

### General Information

Manufacturer of project name \_\_\_\_\_

Collector model no. \_\_\_\_\_

Construction details of the collector:

aperture dimensions and area,  $\text{m}$  and  $\text{m}^2$  ( $\text{ft}$  and  $\text{ft}^2$ ) \_\_\_\_\_

gross dimensions and area,  $\text{m}$  and  $\text{m}^2$  ( $\text{ft}$  and  $\text{ft}^2$ ) \_\_\_\_\_

dimensions and area of absorbing surface,  $\text{m}$  and  $\text{m}^2$  ( $\text{ft}$  and  $\text{ft}^2$ ) \_\_\_\_\_

Absorber area, dimension layout and configuration of flow path, absorptance to short wave radiation (if known), emittance for long wave radiation (if known), description of coating (including maximum allowable temperature (if known),  $^\circ\text{C}$  ( $^\circ\text{F}$ )) \_\_\_\_\_

\*If applicable.

Table 2 - continued

Insulation\*, material, thickness, m (ft), thermal properties \_\_\_\_\_  
\_\_\_\_\_

Transfer liquid used and its thermal and physical properties \_\_\_\_\_  
\_\_\_\_\_

Mass of collector, based on gross area, kg/m<sup>2</sup> (lb/ft<sup>2</sup>) \_\_\_\_\_

Volume of transfer liquid contained in collector, based on gross area  
m<sup>3</sup>/m<sup>2</sup>(ft<sup>3</sup>/ft<sup>2</sup>) \_\_\_\_\_

Direction of flow \_\_\_\_\_

Normal operating temperature range, °C (°F) \_\_\_\_\_

Minimum transfer liquid flow rate, kg/s(lb/h) \_\_\_\_\_

Maximum transfer liquid flow rate, kg/s(lb/h) \_\_\_\_\_

Maximum operating pressure, Pa(lb/ft<sup>2</sup>) \_\_\_\_\_

Description of apparatus used in testing, including flow configuration and instrumentation (include photographs) \_\_\_\_\_

Description of mounting of the collector for testing \_\_\_\_\_

Location of tests (longitude, deg. latitude, deg. and elevation above sea level, m (ft)) \_\_\_\_\_

### Collector Thermal Efficiency Tests

A plot of efficiency vs  $\frac{t_{f,i} - t_a}{I_t}$  \_\_\_\_\_

For each data point:  
 $\dot{m}$  \_\_\_\_\_ kg/s (lb/h) \_\_\_\_\_ J/(kg · °C) (Btu/(lb · °F)) \_\_\_\_\_

$c_p$  \_\_\_\_\_ °C (°F) \_\_\_\_\_

inlet liquid temperature,  $t_{f,i}$  \_\_\_\_\_ °C (°F) \_\_\_\_\_

exit liquid temperature,  $t_{f,e}$  \_\_\_\_\_ °C (°F) \_\_\_\_\_

$T_1$ , time of starting test, \_\_\_\_\_ LST (AST) \_\_\_\_\_

$T_2$ , time of ending test, \_\_\_\_\_ LST (AST) \_\_\_\_\_

$\int_{T_1}^{T_2} (t_{f,e} - t_{f,i}) dT$  \_\_\_\_\_ °C · s (°F · h) \_\_\_\_\_

$\int_{T_1}^{T_2} I_t dT$  \_\_\_\_\_ J/m<sup>2</sup>(Btu/ft<sup>2</sup>) \_\_\_\_\_

pressure drop across the solar collector \_\_\_\_\_ Pa(lb/in.<sup>2</sup>) \_\_\_\_\_

collector tilt angle \_\_\_\_\_ deg. \_\_\_\_\_

collector azimuth angle \_\_\_\_\_ deg. \_\_\_\_\_

incident angle \_\_\_\_\_ deg. \_\_\_\_\_

percentage of incident radiation that is diffuse \_\_\_\_\_ % \_\_\_\_\_

wind speed near the collector surface \_\_\_\_\_ m/s (mph) \_\_\_\_\_

### Collector Incident Angle Modifier Test

Method (1) or Method (2) \_\_\_\_\_

A plot of  $K_{\alpha\tau}$  versus  $\Phi$  \_\_\_\_\_

$(A_a/A_g)F_R(\tau\alpha)_{c,n}$  \_\_\_\_\_

For each data point:  
 $\dot{m}$  \_\_\_\_\_ kg/s(lb/h) \_\_\_\_\_  
 $c_p$  \_\_\_\_\_ J/kg · °C (Btu/(lb · °F)) \_\_\_\_\_

\*If applicable.

**Table 2 - continued**

inlet fluid temperature, $t_{f,i}$	°C (°F)
exit fluid temperature, $t_{f,e}$	°C (°F)
ambient temperature, $t_a$	°C (°F)
$T_1$ , time of starting test	LST (AST)
$T_2$ , time of ending test	LST (AST)
$\int_{T_1}^{T_2} (t_{f,e} - t_{f,i}) dT$	°C·s (°F·h)
$\int_{T_1}^{T_2} I_i dT$	J/m <sup>2</sup> (Btu/ft <sup>2</sup> )
collector tilt angle	deg.
collector azimuth angle	deg.
incident angle	deg.
percentage of incident radiation that is diffuse	%
wind speed near the collector surface or aperture	m/s (mph)

## 10. REFERENCES

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This Appendix is not part of this Standard but is included for information purposes only.

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This Appendix is not part of this Standard but is included for information purposes only.

## APPENDIX B

### Table B1

Solar Position Data for 1977 (values of declination and Equation of Time will vary slightly for specific dates in other years).

Month	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec	
Date													
1	Year Day Declination Eq. of Time	1 -23.0 -3.6	32 -17.0 -13.7	60 -7.4 -12.5	91 +4.7 -4.0	121 +15.2 +2.9	152 +22.1 +2.4	182 +23.1 -3.6	213 +17.9 -6.2	244 +8.2 +0.0	274 -3.3 +10.2	305 -14.6 +16.3	335 -21.9 +11.0
6	Year Day Declination Eq. of Time	6 -22.4 -5.9	37 -15.5 -14.2	65 -5.5 -11.4	96 +6.6 -2.5	126 +16.6 +3.5	157 +22.7 +1.6	187 -22.7 -4.5	218 +16.6 -5.8	249 +6.7 +1.6	279 -5.3 +11.8	310 -16.1 +16.3	340 -22.5 +9.0
11	Year Day Declination Eq. of Time	11 -21.7 -8.0	42 -13.9 -14.4	70 -3.5 -10.2	101 +8.5 -1.1	131 +17.9 +3.7	162 +23.1 +0.6	192 -22.1 -5.3	223 +15.2 -5.1	254 +4.4 +3.3	284 -7.2 -13.1	315 -17.5 +15.9	345 -23.0 +6.3
16	Year Day Declination Eq. of Time	16 -20.8 -9.8	47 -12.2 -4.2	75 -1.6 -8.8	106 +10.3 +0.1	136 +19.2 +3.8	167 +23.3 -0.4	197 +21.3 -5.9	228 +13.6 -4.3	259 +2.5 +5.0	289 -8.7 +14.3	320 -18.8 +15.2	350 -23.3 +4.4
21	Year Day Declination Eq. of Time	21 -19.6 -11.4	52 -10.4 -13.8	80 -7.4	111 +12.0 +1.2	141 +20.3 +3.6	172 +23.4 -1.5	202 +20.6 -6.2	233 +12.0 -3.1	264 +0.5 +6.8	294 -10.8 +15.3	325 -20.0 +14.1	355 -23.4 +2.0
26	Year Day Declination Eq. of Time	26 -18.6 -12.6	57 -8.6 -13.1	85 -5.8	116 +2.4 +2.2	146 +13.6 -3.2	177 +21.2 -2.6	207 +23.3 -6.4	238 +19.3 -1.8	269 +10.3 -8.6	299 -1.4 +15.9	330 -12.6 +12.7	360 -21.0 -0.5

(Units for declination are angular degrees; units for Equation of Time are minutes of time.)

Apparent Solar Time (AST) = local Standard Time ← Eq. of Time + 4 minutes × (Local Standard Time Meridian – Local Longitude).

Standard Time Meridians: EST, 75 deg W

CST, 90 deg W

MST, 105 deg W

PST, 120 deg W

YST, 135 deg W

A-HST 150 deg W

To find solar altitude,  $\beta$ , when latitude L, declination  $\delta$  and hour angle H are known:

$$\sin \beta = \cos L \cos \delta \cos H - \sin L \sin \sigma$$

To find solar azimuth,

$$\sin \phi = \cos \delta \sin H / \cos \beta$$

**Table B2** Solar Position and Insolation\* Values for 24 Degrees North Latitude

NOTE

**NOTE.** \*In these tables "Insolation" denotes solar irradiation.

1. Based on data in Table 1, p. 272 in Ref 2; 0% ground reflectance; 1.0 clarcness factor.

$$1 \text{ Btu}/(\text{ft} \cdot \text{ft}^2) \equiv 3.152 \text{ W/m}^2$$

Table B3 Solar Position and Insolation\* Values for 32 Degrees North Latitude

DATE	SOLAR POSITION			BTU/Hr/SQ. FT. TOTAL INSOLATION ON SURFACES						DATE			SOLAR POSITION			BTU/Hr/SQ. FT. TOTAL INSOLATION ON SURFACES					
	AM	PM	ALT	DIR	NORMAL	SOUTH	FACING	SURFACE ANGLE WITH HORIZ.	AM	PM	ALT	AM	PM	ALT	AM	PM	ALT				
JAN 21	7	5	1.4	65.2	1	0	0	0	1	1	115	115	107.7	113	37	22	14	13	12	8	
	8	4	12.5	56.5	203	56	106	11.6	123	212	181	203	107	87	75	60	44	14	14		
	9	3	22.5	46.0	269	118	193	23.1	167	256	274	221	7	5	23.1	100.6	143	125	104	16	
	10	2	30.6	33.1	295	167	235	35.7	256	308	312	245	8	4	35.7	93.6	158	138	115	31	
	11	1	36.1	17.5	326	198	273	48.4	275	308	321	253	9	3	48.4	85.5	261	231	185	159	
	12		38.0	0.0	310	209	285	10	274	312	324	253	10	2	60.9	74.3	271	269	205	159	
													11	1	72.4	53.3	277	302	262	232	
													11	12	78.6	0.0	279	311	285	256	
																	273	291	242	214	
																	270	293	242	214	
																	270	293	242	214	
FEB 21	7	5	7.1	73.5	121	22	34	40	42	38	37	308	2118	2186	1779	11	12	302	310	285	256
	8	4	19.0	64.4	247	95	127	136	140	141	108	108	108	108	12	12	310	311	296	256	
	9	3	29.9	53.4	288	161	206	217	222	220	158	158	158	158	11	12	302	312	297	256	
	10	2	39.1	39.4	306	212	266	278	283	279	193	193	193	193	7	5	19.1	92.8	190	144	
	11	1	45.6	21.4	315	244	304	317	321	315	214	214	214	214	8	4	31.8	84.7	240	156	
	12		48.0	0.0	317	255	316	330	334	328	222	222	222	222	9	3	44.3	75.0	263	216	
																	10	2	56.1	276	
																	11	1	66.0	282	
																	11	1	76.4	298	
																	12	1	86.0	305	
																	12	1	96.0	317	
																	12	1	106.0	324	
MAR 21	7	5	12.7	81.9	185	60	60	59	56	52	32	32	32	32	11	12	5	12.7	81.9	163	
	8	4	25.1	73.0	260	129	146	147	144	137	78	78	78	78	7	5	25.1	73.0	240	141	
	9	3	36.8	62.1	290	194	222	224	220	209	119	119	119	119	150	150	12.7	81.9	163	56	
	10	2	47.3	47.5	304	245	280	283	278	265	170	170	170	170	150	150	8	4	25.1	56	
	11	1	55.0	26.8	311	277	317	321	315	300	170	170	170	170	170	170	9	3	36.8	62.1	
	12		58.0	0.0	313	287	329	333	327	312	177	177	177	177	177	177	10	2	47.3	57.5	
																	11	1	55.0	26.8	
																	11	12	58.0	0.0	
																	12	1	68.0	296	
																	12	1	78.0	305	
																	12	1	88.0	314	
																	12	1	98.0	323	
APR 21	6	6	6.1	99.9	92.2	206	86	78	71	62	51	10	136	120	35	35	7	5	12.7	81.9	163
	7	5	18.8	84.0	278	220	225	217	203	183	68	68	68	68	170	170	8	4	25.1	73.0	240
	8	4	31.5	43.9	279	267	272	279	256	234	95	95	95	95	170	170	9	3	29.5	73.0	240
	9	3	43.9	74.2	290	260	273	271	250	233	108	108	108	108	170	170	10	2	30.8	73.0	240
	10	2	55.7	60.3	295	295	313	306	290	277	112	112	112	112	170	170	11	1	39.1	73.0	240
	11	1	65.4	37.5	307	307	325	318	301	293	118	118	118	118	170	170	11	1	45.1	73.0	240
	12		69.6	0.0	296	315	315	301	278	247	77	77	77	77	170	170	11	12	47.5	0.0	304
																	12	1	56.0	296	
																	12	1	66.0	305	
																	12	1	76.0	314	
																	12	1	86.0	323	
																	12	1	96.0	332	
MAY 21	6	6	10.4	107.2	119	36	21	107	88	75	44	44	13	13	12	12	7	5	12.7	81.9	163
	7	5	22.8	100.1	211	107	88	75	60	44	13	13	13	13	105	105	8	4	25.1	73.0	240
	8	4	35.4	92.9	250	175	159	145	127	105	15	15	15	15	105	105	9	3	29.5	73.0	240
	9	3	48.1	84.7	269	233	223	209	188	163	33	33	33	33	105	105	8	2	30.8	73.0	240
	10	2	60.6	73.3	280	277	273	259	257	237	56	56	56	56	105	105	9	1	39.1	73.0	240
	11	1	72.0	51.9	285	305	305	290	288	268	72	72	72	72	105	105	10	2	30.8	73.0	240
	12		78.0	0.0	286	315	315	301	278	247	77	77	77	77	105	105	11	1	36.2	73.0	240
																	11	1	45.1	73.0	
																	11	12	38.2	0.0	
																	12	1	56.0	296	
																	12	1	66.0	305	
																	12	1	76.0	314	
JUN 21	6	6	12.2	110.2	131	45	26	16	15	14	9	9	14	14	12	12	7	5	12.7	81.9	163
	7	5	24.3	103.4	210	115	91	76	59	41	14	14	14	14	12	12	8	4	25.1	73.0	240
	8	4	36.9	96.8	245	180	159	143	122	99	16	16	16	16	10	10	9	3	29.5	73.0	240
	9	3	49.6	89.4	264	236	221	204	181	153	19	19	19	19	10	10	10	2	30.8	73.0	240
	10	2	62.2	79.7	274	279	268	251	227	197	1	1	1	1	11	11	11	1	32.7	73.0	240
	11	1	74.2	60.9	280	315	309	299	282	257	56	56	56	56	11	11	11	12	34.6	0.0	304
	12		81.5	0.0	280	315	309	299	282	257	77	77	77	77	11	11	11	12	34.6	0.0	304
																	11	1	45.1	73.0	
																	11	12	38.2	0.0	
																	12	1	56.0	296	
																	12	1	66.0	305	
																	12	1	76.0	314	

NOTE:

\*In these tables "Insolation" denotes solar irradiation.

1. Based on data in Table I, p. 27.2 in Ref 2; 0% ground reflectance; 1.0 clearness factor.

2. See Fig. 3, p. 27.3 in Ref 2 for typical regional clearness factors.

1 BTU/(h · ft<sup>2</sup>) = 3.152 W/m<sup>2</sup>

Table B4 Solar Position and Insolation\* Values for 40 Degrees North Latitude

DATE	SOLAR POSITION			BTU/HR. SQ. FT. TOTAL INSOLATION ON SURFACES			SOLAR POSITION			BTUH/SQ. FT. TOTAL INSOLATION ON SURFACES ANGLE WITH HORIZ.		
	AM	PM	ALT	SOUTH FACING SURFACE ANGLE WITH HORIZ.			AM	PM	ALT	SOUTH FACING SURFACE ANGLE WITH HORIZ.		
				NORMAL	HORIZ.	50°	50°	40°	30°	NORMAL	HORIZ.	50°
JUN 21	8	4	8.1	55.3	142	28	81	85	84	115.2	2	0
	9	3	16.8	44.0	239	83	155	171	182	106.1	50	0
	10	2	23.8	30.9	274	127	218	237	249	97.2	26	17
	11	1	28.4	16.0	289	154	257	277	290	87.8	114	15
	12	0	30.0	0.0	294	164	270	291	303	241	174	14
				SURFACE DAILY TOTALS	21882	948	1660	1810	1906	1944	1726	182
FEB 21	7	5	4.8	72.7	69	10	19	21	23	76.7	225	203
	8	4	15.4	62.2	224	73	114	122	126	76.7	225	203
	9	3	25.0	50.2	274	132	195	205	209	76.7	225	203
	10	2	32.8	35.9	295	178	256	267	271	76.7	225	203
	11	1	38.1	18.9	305	206	293	306	310	76.7	225	203
	12	0	40.0	0.0	318	216	306	319	323	76.7	225	203
MAR 21	7	5	11.4	80.2	171	46	55	54	55	107	276	254
	8	4	22.5	69.6	250	114	140	141	138	107	276	254
	9	3	32.8	57.3	282	173	215	217	213	107	276	254
	10	2	41.6	41.9	297	218	273	276	271	107	276	254
	11	1	47.7	22.6	305	247	310	313	307	107	276	254
	12	0	50.0	0.0	307	247	310	313	307	107	276	254
APR 21	6	6	7.4	98.9	89	20	11	8	7	114	202	184
	7	5	18.9	89.5	206	87	77	76	61	114	202	184
	8	4	30.3	79.3	252	152	153	145	133	114	202	184
	9	3	40.3	67.2	274	207	221	213	199	93	202	184
	10	2	51.2	51.4	286	250	275	267	252	126	202	184
	11	1	58.7	29.2	292	277	308	301	285	147	202	184
MAY 21	5	7	1.9	114.7	1	0	0	0	0	102	218	196
	6	6	12.7	105.6	144	49	25	15	14	136	218	196
	7	5	24.0	96.6	216	214	89	76	60	136	218	196
	8	4	35.4	87.2	250	175	158	144	125	136	218	196
	9	3	46.8	76.0	267	227	221	206	186	136	218	196
	10	2	57.5	60.9	277	270	255	233	205	136	218	196
JUN 21	9	3	66.2	57.1	283	301	287	264	234	108	218	196
	10	2	70.0	0.0	284	301	312	297	274	114	218	196
	11	1	69.2	41.9	277	272	266	248	222	194	218	196
	12	0	73.5	0.0	279	304	306	289	263	192	218	196
				SURFACE DAILY TOTALS	3180	2552	2442	2264	2040	1760	724	196
				SURFACE DAILY TOTALS	3180	2552	2442	2264	2040	1760	724	196

NOTE:

\*In these tables "Insolation" denotes solar irradiation.

1. Based on data in Table I, p. 27.2, in Ref 2; 0% ground reflectance; 1.0 clearness factor.

2. See Fig. 3, p. 27.3 in Ref 2 for typical regional clearness factors.

1 BTU/(h · ft<sup>2</sup>) = 3.152 W/m<sup>2</sup>

Table B5 Solar Position and Insolation\* Values for 48 Degrees North Latitude

DATE	SOLAR TIME AM	SOLAR POSITION		BTU/H. SQ. FT. TOTAL INSOLATION ON SURFACES						DATE	SOLAR TIME AM	SOLAR POSITION		BTU/H. SQ. FT. TOTAL INSOLATION ON SURFACES								
		ALT	AZM	DIRECT NORMAL			SOUTH FACING SURFACE ANGLE WITH HORIZ.						ALT	AZM	NORMAL			HORIZ.				
				HORIZ.	45°	38°	48°	58°	68°			45°			38°	48°	58°	68°				
JAN 21	8	4	3.5	54.6	37	4	17	19	21	22	21	5	7	5.7	114.7	10	5	4	3			
	9	3	11.0	42.6	185	46	120	132	140	145	139	6	6	15.2	104.1	156	28	18	15			
	10	2	16.9	29.4	239	83	190	206	216	220	206	7	5	25.1	93.5	211	89	75	42			
	11	1	20.7	15.1	261	107	231	249	260	243	243	8	4	35.1	82.1	240	154	140	11			
	12		22.0	0.0	267	115	245	264	275	255	255	9	3	44.8	68.8	256	215	199	99			
			SURFACE DAILY TOTALS		1710	596	1360	1478	1550	1578	1478	10	2	52.5	51.9	266	250	246	153			
FEB 21	7	5	2.4	72.2	12	1	3	4	4	4	4	11	1	60.1	29.0	271	291	276	225			
	8	4	11.6	60.5	188	49	95	102	105	106	96	12	1	62.6	0.0	272	279	301	286			
	9	3	19.7	47.7	251	100	178	187	191	190	167					279	301	286	232			
	10	2	26.2	33.3	278	139	240	251	255	251	217					277	315	286	244			
	11	1	30.5	17.2	290	165	278	290	294	288	247					274	318	286	244			
	12		SURFACE DAILY TOTALS		293	173	291	304	307	301	258	8	4	29.0	75.4	232	141	145	20			
MAR 21	7	5	10.0	78.7	2350	1080	1860	1972	2074	1978	1720	9	3	38.4	61.8	189	210	201	110			
	8	4	19.5	66.8	153	37	49	40	47	45	35	10	2	46.4	45.1	225	260	252	237			
	9	3	28.2	55.4	217	147	205	207	203	195	152	11	1	52.2	24.3	248	293	285	244			
	10	2	35.4	37.8	287	187	263	266	261	248	195	12	1	54.3	0.0	274	256	256	244			
	11	1	40.3	19.8	295	212	300	307	297	283	223					2898	2086	2300	2200			
	12		SURFACE DAILY TOTALS		298	220	315	315	309	294	232	8	4	39.5	78.7	131	35	44	31			
APR 21	6	6	8.6	97.8	2780	1578	2208	2228	2282	2074	1632	9	3	28.2	66.8	215	92	124	115			
	7	5	18.6	86.7	205	85	76	69	59	48	21	10	2	55.4	53.4	142	196	197	143			
	8	4	28.5	74.9	247	142	149	141	129	113	69	11	1	40.3	40.3	181	251	254	205			
	9	3	37.8	61.2	268	191	216	208	194	174	115					42.0	0.0	280	213			
	10	2	45.8	44.6	280	228	260	260	245	223	152					280	213	299	221			
	11	1	51.5	24.0	286	252	301	294	278	254	177					287	205	289	212			
	12		SURFACE DAILY TOTALS		288	260	313	305	289	264	185	9	3	19.3	25.7	133	228	239	207			
MAY 21	5	7	5.2	114.3	3016	2106	2258	2266	2114	1902	1262	10	2	25.7	33.1	262	157	266	277			
	6	6	14.7	103.7	41	9	4	4	3	2	115	11	1	30.0	17.1	274	291	276	237			
	7	5	24.5	93.0	219	118	89	75	60	43	13					31.5	0.0	278	279			
	8	4	34.7	81.6	248	171	156	142	123	101	45					31.5	0.0	286	287			
	9	3	44.3	68.3	264	217	217	202	182	156	86	9	3	11.2	42.7	94	167	176	157			
	10	2	53.0	51.3	274	252	265	251	229	200	120	10	2	17.1	29.5	233	133	228	221			
	11	1	59.5	28.6	279	274	296	281	258	228	141	11	1	20.9	15.1	107	227	245	215			
	12		SURFACE DAILY TOTALS		280	281	306	292	269	238	149	12	1	22.2	0.0	261	115	241	250			
JUN 21	5	7	7.9	116.5	3254	2482	2918	2234	2010	1728	982	5				1688	596	1336	154			
	6	6	17.2	106.2	77	21	9	8	7	5	DEC 21	9	3	8.0	40.9	140	27	87	105			
	7	5	27.0	95.8	74	33	19	18	16	12	10	2	13.6	28.2	63	164	180	197				
	8	4	37.1	84.6	246	129	93	77	59	39	11	1	17.3	14.4	242	86	207	226				
	9	3	46.9	71.6	261	181	157	140	119	95	35	12	18.6	0.0	250	94	222	244				
	10	2	55.8	54.8	269	259	262	244	223	200	147	74				1444	446	1136	1364			
	11	1	62.7	31.2	274	280	291	273	248	216	105					1444	446	1136	1364			
	12		SURFACE DAILY TOTALS		65.5	0.0	275	287	301	283	258	225	133									

NOTE:

\*In these tables "Insolation" denotes solar irradiation.

1. Based on data in Table I, p. 27-2 in Ref 2; 0% ground reflectance; 1.0 clearness factor.
2. See Fig. 3, p. 27-3 in Ref 2 for typical regional clearness factors.

$$1 \text{ BTU}/(\text{hr} \cdot \text{ft}^2) = 3.152 \text{ W/m}^2$$

Table B6 Solar Position and Insolation\* Values for 56 Degrees North Latitude

DATE	SOLAR POSITION			BTU/SD. FT. TOTAL INSOLATION ON SURFACES			DATE			SOLAR POSITION			BTU/SD. FT. TOTAL INSOLATION ON SURFACES											
	AM	PM	ALT	DIRECT	NORMAL	AZIM	SOUTH FACING SURFACE ANGLE WITH HORIZ.	HORIZ.	66	66	76	AM	PM	ALT	AZIM	SOUTH FACING SURFACE ANGLE WITH HORIZ.	HORIZ.	46	56	66	76			
JUN 21	9	3	5.0	41.8	78	11	50	55	60	60	60	JUL 21	4	8	1.7	125.8	0	0	0	0	0	0	0	
10	2	9.9	28.5	170	39	135	146	154	156	153	153	5	7	9.0	113.7	91	27	11	10	9	8			
11	1	12.9	14.5	207	58	183	197	206	208	201	201	6	6	17.0	101.9	169	72	50	18	16	14			
12		14.0	0.0	217	65	198	214	222	225	217	217	7	5	25.3	89.7	212	119	88	74	58	41			
SURFACE DAILY TOTALS			1126	282	924	1010	1058	1074	1094	1094	1094	SURFACE DAILY TOTALS			8	4	33.6	76.7	237	151	136	117		
JUL 21	8	4	7.6	59.4	129	25	65	69	72	69	69	JUL 21	4	8	1.7	125.8	0	0	0	0	0	0	0	
10	2	19.4	31.5	250	98	215	225	228	224	211	211	10	2	41.4	62.0	252	201	208	193	173	147			
11	1	22.8	16.1	265	119	254	265	268	263	243	243	11	1	48.2	44.6	261	230	254	239	217	185			
12		24.0	0.0	270	126	268	279	282	276	255	255	12	1	52.9	23.7	265	248	283	268	216	166			
SURFACE DAILY TOTALS			1986	740	1940	1716	1742	1716	1598	1598	1598	SURFACE DAILY TOTALS			8	4	109.2	112	34	16	11	10		
MAR 21	7	5	8.3	77.5	128	28	40	39	37	37	37	JULY 21	5	7	2.0	109.2	1	0	0	0	0	0	0	
8	4	16.6	64.4	215	75	119	120	117	111	97	97	6	6	10.2	97.0	112	34	16	11	10	9			
9	3	23.3	50.3	253	118	192	193	189	180	154	154	7	5	18.5	84.5	187	82	73	65	56	45			
10	2	29.0	34.9	272	151	249	251	246	234	205	205	8	4	26.7	71.3	225	128	140	131	119	106			
11	1	32.7	17.9	282	172	285	288	282	268	236	236	9	3	34.3	56.7	246	108	202	193	179	160			
12		34.0	0.0	284	179	297	300	294	280	246	246	10	2	40.5	40.0	258	199	251	242	227	205			
SURFACE DAILY TOTALS			2586	1268	2066	2084	2040	1938	1700	1700	1700	SURFACE DAILY TOTALS			11	1	44.8	20.9	282	218	282	235		
APR 21	5	7	1.4	108.8	0	0	0	0	0	0	0	JULY 21	5	7	2.0	109.2	1	0	0	0	0	0	0	
6	6	9.6	96.5	122	32	14	9	8	7	6	6	SURFACE DAILY TOTALS	7	5	8.3	77.5	107	25	36	36	34	32	29	
7	5	18.0	84.1	201	81	74	66	57	46	29	29	SURFACE DAILY TOTALS	8	4	4	64.4	194	72	111	111	108	102	85	
8	4	26.1	70.9	239	129	143	135	123	108	82	82	SURFACE DAILY TOTALS	9	3	13.8	45.7	233	114	181	182	178	168	149	
9	3	33.6	56.3	260	169	208	200	186	167	133	133	SURFACE DAILY TOTALS	10	2	23.3	50.3	253	146	236	237	221	221	200	
10	2	39.9	39.7	272	201	259	251	236	214	174	174	SURFACE DAILY TOTALS	11	1	32.7	17.9	263	166	271	273	267	254	222	
11	1	44.1	20.7	278	220	292	284	268	245	200	200	SURFACE DAILY TOTALS	12	1	34.0	0.0	286	173	285	285	279	265	235	
SURFACE DAILY TOTALS			3024	1892	2282	2186	2038	1830	1458	1458	1458	SURFACE DAILY TOTALS			10	7	59.1	59.1	104	20	53	57	59	59
MAY 21	4	8	1.2	125.5	0	0	0	0	0	0	0	JULY 21	5	7	8.3	77.5	107	25	36	36	34	32	29	
5	7	8.5	113.4	93	25	10	9	8	7	6	6	SURFACE DAILY TOTALS	9	3	13.8	45.7	193	60	145	145	146	147	136	
6	6	16.5	101.5	175	71	28	17	15	13	11	11	SURFACE DAILY TOTALS	10	2	19.0	31.3	231	92	201	210	213	210	195	
7	5	24.8	89.3	219	119	88	74	58	41	16	16	SURFACE DAILY TOTALS	11	1	22.3	16.0	248	112	240	250	253	248	230	
8	4	33.1	76.3	244	163	153	138	119	98	63	63	SURFACE DAILY TOTALS	12	1	23.5	0.0	253	119	253	263	266	261	241	
9	3	40.9	61.6	259	201	212	197	176	151	109	109	SURFACE DAILY TOTALS	13	1	41.9	41.9	49	54	54	59	59	58	56	
10	2	47.6	44.2	268	231	259	244	222	194	146	146	SURFACE DAILY TOTALS	14	1	10.0	28.5	165	39	132	143	143	149	144	
11	1	52.3	23.4	273	249	288	274	251	222	170	170	SURFACE DAILY TOTALS	15	1	14.5	20.1	201	58	179	193	201	203	196	
SURFACE DAILY TOTALS			3340	2374	2374	2188	1962	1682	1218	1218	1218	SURFACE DAILY TOTALS			11	12	14.7	0.0	211	65	194	209	217	219
JUN 21	4	8	4.2	127.2	21	4	2	2	2	1	1	JULY 21	5	7	1.9	109.4	284	94	3	4	4	4	4	
5	7	11.4	115.3	122	40	14	13	11	10	8	8	SURFACE DAILY TOTALS	10	2	6.6	27.5	113	19	86	95	101	104	103	
6	6	19.3	103.6	185	86	54	39	19	17	15	15	SURFACE DAILY TOTALS	11	1	9.5	13.9	166	37	141	154	163	167	164	
7	5	27.6	91.7	222	132	92	76	57	38	154	154	SURFACE DAILY TOTALS	12	1	10.6	0.0	180	43	159	173	182	186	187	
8	4	35.9	78.8	243	175	212	211	193	170	143	143	SURFACE DAILY TOTALS	13	1	14.5	98	184	214	242	210	156	120		
9	3	43.8	64.1	257	212	211	204	255	240	265	265	SURFACE DAILY TOTALS	14	1	24.8	284	284	267	267	219	164	116		
10	2	50.7	46.4	265	240	255	238	214	184	133	133	SURFACE DAILY TOTALS	15	1	26.6	264	264	263	263	216	166	116		
11	1	55.6	24.9	269	258	284	274	242	210	156	156	SURFACE DAILY TOTALS	16	1	27.4	264	264	263	263	216	166	116		
SURFACE DAILY TOTALS			3438	2562	2388	2188	1910	1606	120	120	120	SURFACE DAILY TOTALS			17	18	18.6	18.6	18.6	17.4	17.4	17.4		

NOTE:

\*In these tables "Insolation" denotes solar irradiation.

1. Based on data in Table I, p. 27.2 in Ref 2; 0% ground reflectance, 1.0 clearness factor.

2. See Fig. 3, p. 27.3 in Ref 2 for typical regional clearness factors.

1 BTU/(hr · ft<sup>2</sup>) = 3.152 W/m<sup>2</sup>

Table B7 Solar Position and Insolation<sup>\*</sup> Values for 64 Degrees North Latitude

DATE	SOLAR POSITION			BTU/SQ. FT. TOTAL INSOLATION ON SURFACES						DATE	SOLAR TIME			BTU/SQ. FT. TOTAL INSOLATION ON SURFACES								
	AM	PM	ALT	AZN	DIRECT	NORMAL	SOUTH	FACING	SURFACE	ANGLE	AM	PM	ALT	AZN	DIRECT	NORMAL	SOUTH	FACING	SURFACE	ANGLE		
JAN 21	10	2	28	28.1	22	2	17	19	20	20	90	54	5	5	6	6.4	125.3	53	13	6	5	4
11	1	5.2	14.1	14.1	81	12	72	77	80	81	90	54	4	4	14	12.1	112.4	44	13	11	10	9
12		6.0	0.0	100	16	91	98	102	103	103	103	54	7	7	6	18.4	99.4	179	81	30	17	12
SURFACE DAILY TOTALS				396	45	268	290	302	306	304	90	54	7	7	5	25.0	86.0	211	118	86	72	56
FEB 21	8	4	3.4	58.7	35	4	17	19	19	19	90	54	7	7	5	25.0	86.0	231	152	146	131	91
9	3	8.6	44.8	44.8	147	51	103	108	111	110	107	54	8	8	4	31.4	71.8	245	182	186	166	124
10	2	12.6	30.3	30.3	199	55	170	178	181	178	173	54	9	9	3	37.3	56.3	253	204	245	230	162
11	1	15.1	15.1	15.1	222	71	212	220	223	219	213	54	10	2	2	42.2	39.2	253	215	273	236	167
12		16.0	0.0	228	77	225	235	237	232	226	11	54	1	1	20.2	45.4	211	152	259	212	216	
SURFACE DAILY TOTALS				1452	400	1290	1286	1292	1282	1252	90	54	12	12	0.0	46.6	223	282	267	245	216	195
MAR 21	7	5	6.5	76.5	95	18	30	29	29	29	29	54	7	7	4.6	108.8	3572	2280	2090	1864	1588	1490
8	4	20.7	62.6	62.6	185	54	101	102	99	94	89	54	6	6	11.0	95.5	123	39	16	11	2	2
9	3	18.1	48.1	48.1	227	87	171	172	169	160	153	54	7	5	17.6	91.9	181	77	69	63	52	55
10	2	22.3	32.7	32.7	249	112	227	229	224	213	203	54	8	4	23.9	67.8	214	113	132	123	112	107
11	1	25.1	16.6	16.6	260	129	252	265	259	246	235	54	9	3	29.6	52.6	234	144	190	162	169	150
12		26.0	0.0	0.0	263	134	274	277	271	268	246	54	10	2	34.2	36.2	246	168	257	225	215	194
SURFACE DAILY TOTALS				2296	932	1856	1870	1850	1736	1656	90	54	11	1	37.2	18.5	252	183	268	260	222	205
APR 21	5	7	4.0	108.5	27	5	2	2	2	1	1	54	12	12	0.0	254	188	273	270	255	255	255
6	6	10.4	95.1	95.1	133	37	15	9	8	8	7	54	6	6	4.6	108.8	2006	1606	1460	1362	1372	1352
7	5	17.0	81.6	81.6	194	76	70	63	54	43	37	54	7	5	6.5	76.5	77	16	25	25	23	21
8	4	23.3	67.5	67.5	228	112	136	128	116	102	91	54	8	4	12.7	72.6	163	51	92	92	80	71
9	3	29.0	52.3	52.3	248	144	197	189	176	158	145	54	9	3	18.1	48.1	206	83	159	159	156	141
10	2	33.5	36.0	36.0	260	169	246	239	224	203	188	54	10	2	22.3	32.7	229	108	212	213	209	196
11	1	36.5	18.4	18.4	266	184	278	270	255	233	216	54	11	1	25.1	16.6	240	124	246	235	230	220
12		97.6	0.0	0.0	268	190	289	281	266	243	225	54	12	12	0.0	284	129	258	250	250	251	250
SURFACE DAILY TOTALS				2382	1264	2176	2082	1936	1736	1594	90	54	6	6	3.0	58.5	2074	1820	1726	1636	1638	1552
MAY 21	4	8	5.8	125.1	51	11	5	4	3	3	3	54	8	8	4	3.0	58.5	17	2	9	9	10
5	7	11.6	112.1	112.1	132	42	13	11	10	9	8	54	9	3	8.1	44.6	122	26	86	91	92	90
6	6	17.9	99.1	99.1	185	79	29	16	14	12	11	54	10	2	12.1	30.2	176	50	152	159	161	155
7	5	24.5	85.7	85.7	218	117	86	72	56	39	28	54	11	1	1	15.2	20.1	201	65	193	203	203
8	4	30.9	71.5	71.5	239	152	148	133	115	99	80	54	12	1	15.5	0.0	208	71	207	215	213	208
9	3	36.8	56.1	56.1	252	182	204	190	170	145	128	54	13	1	12.3	12.3	123	1136	1134	1116	1116	1116
10	2	41.6	38.9	38.9	261	205	249	235	213	186	167	54	10	2	3.0	28.1	23	3	18	20	21	21
11	1	44.9	20.1	20.1	265	219	278	264	242	213	193	54	11	1	5.4	14.2	79	12	80	80	80	79
12		46.0	0.0	0.0	267	224	284	274	251	222	201	54	12	12	6.2	0.0	97	12	80	80	80	79
SURFACE DAILY TOTALS				2470	2236	2312	2124	1898	1624	1436	90	54	2	2	2	2	302	266	286	286	302	300
JUN 21	3	9	4.2	139.4	21	4	2	2	2	2	2	54	8	7	6	1.8	13.7	4	0	3	4	4
4	8	9.0	126.4	93	27	10	9	8	7	6	54	11	10	10	2.6	0.0	16	2	15	16	17	
5	7	14.7	113.6	154	60	194	96	34	19	15	13	54	11	11	11	2.6	0.0	20	22	24	24	24
6	6	21.0	100.8	100.8	221	132	91	74	55	36	20	54	11	14	14	14	0.0	101	101	101	101	101
7	5	27.5	87.5	87.5	239	166	150	133	112	88	73	54	12	12	12	12	0.0	23	23	23	23	23
8	4	34.0	73.3	73.3	251	195	204	187	164	137	119	54	13	13	13	13	0.0	23	23	23	23	23
9	3	39.9	57.8	57.8	258	217	247	230	206	177	157	54	14	14	14	14	0.0	23	23	23	23	23
10	2	44.9	40.4	40.4	262	231	275	253	233	207	181	54	15	15	15	15	0.0	23	23	23	23	23
11	1	48.5	20.9	20.9	263	225	284	267	242	211	181	54	16	16	16	16	0.0	23	23	23	23	23
12		49.5	0.0	0.0	2650	2342	2118	1862	1558	1356	1356	54	21	21	21	21	0.0	23	23	23	23	23

NOTE:

\*In these tables "Insolation" denotes solar irradiation.

1. Based on data in Table I, p. 27.2 in Ref 2; 0% ground reflectance; 1.0 clearness factor.

2. See Fig. 3, p. 27.3 in Ref 2 for typical regional clearness factors.

1 BTU/(h · ft<sup>2</sup>) = 3.152 W/m<sup>2</sup>

**Table B8 Latitude 24°N, Incident Angles for Horizontal and South-Facing Tilted Surfaces**

Dates (Declination)	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Dec. 21 (-23.45)	7	5	86.8	80.5	76.3	72.4	68.9	62.6
	8	4	75.1	67.5	62.7	58.6	55.4	56.6
	9	3	64.5	55.3	49.6	44.9	41.8	51.1
	10	2	55.7	44.5	37.4	31.6	28.0	46.6
	11	1	49.6	36.5	27.6	19.6	14.3	43.6
	12		47.4	33.4	23.5	13.5	3.4	42.5
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jan. 21 (-19.9)	7	5	85.2	79.6	75.9	72.6	69.8	65.7
	8	4	73.1	66.2	62.0	58.5	56.0	59.9
	9	3	62.1	53.5	48.4	44.5	42.2	54.4
	10	2	52.8	42.1	35.5	30.6	28.2	50.0
	11	1	46.4	33.4	24.8	17.6	14.1	47.0
	12		44.0	30.0	20.0	10.0	0.0	46.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Feb. 21 (-10.6)	7	5	80.7	77.2	75.2	73.7	72.6	74.8
	8	4	67.7	62.9	60.5	59.0	58.5	69.0
	9	3	55.6	49.0	45.9	44.3	44.5	63.8
	10	2	44.9	35.9	31.5	29.5	30.6	59.6
	11	1	37.0	25.0	18.0	14.8	17.6	56.9
	12		34.0	20.0	10.0	0.0	10.0	56.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Mar. 21 (0.0)	7	5	76.3	75.2	75.0	75.2	75.9	84.0
	8	4	62.8	60.5	60.0	60.5	62.0	78.3
	9	3	49.8	45.9	45.0	45.9	48.4	73.3
	10	2	37.7	31.5	30.0	31.5	35.5	69.4
	11	1	28.1	18.0	15.0	18.0	24.8	66.9
	12		24.0	10.0	0.0	10.0	20.0	66.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Apr. 21 (+11.9)	6	6	85.3	88.0	90.0	92.0	93.9	100.6
	7	5	71.7	73.5	75.3	77.6	80.2	94.6
	8	4	58.0	58.9	60.7	63.4	67.0	89.1
	9	3	44.4	44.2	46.2	49.7	54.4	84.4
	10	2	31.0	29.5	32.0	36.8	43.2	80.7
	11	1	18.9	14.8	18.9	26.2	34.9	78.4
	12		12.4	1.6	11.6	21.6	31.6	77.6
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
May 21 (+20.3)	6	6	82.0	86.0	90.0	93.4	96.7	108.2
	7	5	68.8	72.6	75.9	79.6	83.6	102.3
	8	4	55.4	58.5	62.0	66.2	71.1	97.0
	9	3	41.7	44.5	48.4	53.5	59.5	92.4
	10	2	28.0	30.6	35.5	42.1	49.6	88.9
	11	1	14.5	17.6	24.8	33.4	42.6	86.7
	12		4.0	10.0	20.0	30.0	40.0	86.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jun. 21 (+23.45)	6	6	80.7	86.0	90.0	94.0	97.8	111.3
	7	5	67.7	72.4	76.3	80.5	85.0	105.5
	8	4	54.5	58.6	62.7	67.5	72.8	100.2
	9	3	41.0	44.9	49.6	55.8	61.7	95.7
	10	2	27.4	31.6	37.4	44.5	52.4	92.3
	11	1	13.7	19.7	27.6	36.5	45.9	90.2
	12		0.6	13.4	23.4	33.4	43.4	89.4

**Table B9 Latitude 32°N, Incident Angles for Horizontal and South-Facing Tilted Surfaces**

Dates (Declination)	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Dec. 21 (-23.45)	8	4	79.7	67.5	62.7	58.6	55.4	54.5
	9	3	70.2	55.3	49.6	44.9	41.8	47.1
	10	2	62.4	44.5	37.4	31.6	28.0	40.7
	11	1	57.3	36.5	27.6	19.6	14.3	36.2
	12		55.4	33.4	23.4	13.5	3.5	34.5
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jan. 21 (-19.9)	7	5	88.6	79.6	75.9	72.6	69.8	65.2
	8	4	77.5	66.2	62.0	58.5	56.0	57.4
	9	3	67.5	53.5	48.4	44.5	42.2	50.0
	10	2	59.4	42.1	35.5	30.6	28.2	43.8
	11	1	53.9	33.4	24.8	17.6	14.1	39.6
	12		52.0	30.0	20.0	10.0	6.0	38.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Feb. 21 (-10.6)	7	5	82.9	77.2	75.2	73.7	72.6	73.6
	8	4	71.0	62.9	60.5	59.0	58.5	65.9
	9	3	60.1	49.0	45.9	44.3	44.5	58.9
	10	2	50.9	35.9	31.5	29.5	30.6	53.2
	11	1	44.4	25.0	18.0	14.8	17.6	49.4
	12		42.0	20.0	10.0	0.0	10.0	48.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Mar. 21 (0.0)	7	5	77.3	75.2	75.0	75.2	75.9	82.1
	8	4	64.9	60.5	60.0	60.5	62.0	74.6
	9	3	53.2	45.9	45.0	45.9	48.4	68.0
	10	2	42.7	31.5	30.0	31.5	35.5	62.7
	11	1	35.0	18.0	15.0	18.0	24.8	59.2
	12		32.0	10.0	0.0	10.0	20.0	58.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Apr. 21 (+11.9)	6	6	83.9	88.0	90.0	92.0	93.9	99.8
	7	5	71.2	73.5	75.3	77.6	80.2	92.1
	8	4	58.5	58.9	60.7	63.4	67.0	84.9
	9	3	46.1	44.2	46.2	49.7	54.4	78.7
	10	2	34.3	29.5	32.0	36.8	43.2	73.8
	11	1	24.6	14.8	18.9	26.2	34.9	70.7
	12		20.4	1.6	11.6	21.6	31.6	69.6
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
May 21 (+20.3)	6	6	79.6	86.6	90.0	93.4	96.7	106.9
	7	5	67.2	72.6	75.9	79.6	83.6	99.3
	8	4	54.6	58.5	62.0	66.2	71.1	92.4
	9	3	41.9	44.5	48.4	53.5	59.5	86.4
	10	2	29.4	30.6	35.5	42.1	49.6	81.9
	11	1	18.0	17.6	24.8	33.4	42.6	79.0
	12		12.0	10.0	20.0	30.0	40.0	78.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jun. 21 (+23.45)	6	6	77.8	86.0	90.0	94.0	97.8	109.7
	7	5	65.7	72.4	76.3	80.5	85.0	102.2
	8	4	53.1	58.6	62.7	67.5	72.8	93.4
	9	3	40.4	44.9	49.6	55.3	61.7	89.6
	10	2	27.8	31.6	37.4	44.5	52.4	85.2
	11	1	15.8	19.6	27.6	36.5	45.8	82.4
	12		8.6	13.4	23.4	33.4	43.4	81.4

**Table B10 Latitude 40°N, Incident Angles for Horizontal and South-Facing Tilted Surfaces**

Dates (Declination)	am	pm	Horiz.	L. - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Dec. 21 (-23.45)	8	4	84.5	67.5	62.7	58.6	55.4	53.2
	9	3	76.0	55.3	49.6	44.9	41.8	43.8
	10	2	69.3	44.5	37.4	31.6	28.0	35.4
	11	1	65.0	36.5	27.6	19.6	14.3	29.0
	12		63.4	33.4	23.4	13.5	3.5	26.6
	am	pm	Horiz.	L. - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jan. 21 (-19.9)	8	4	81.9	66.2	62.0	58.5	56.0	55.7
	9	3	73.2	53.5	48.4	44.5	42.2	46.4
	10	2	66.2	42.1	35.5	30.6	28.2	38.3
	11	1	61.6	33.4	24.8	17.6	14.1	32.3
	12		60.0	30.0	20.0	10.0	0.0	30.0
	am	pm	Horiz.	L. - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Feb. 21 (-10.6)	7	5	85.2	77.2	75.2	73.7	72.6	72.7
	8	4	74.6	62.9	60.5	59.0	58.5	63.3
	9	3	65.0	49.0	45.9	44.3	44.5	59.5
	10	2	57.2	35.9	31.5	29.5	30.6	47.1
	11	1	51.9	25.0	18.0	14.8	17.6	49.9
	12		50.0	20.0	10.0	0.0	10.0	40.0
	am	pm	Horiz.	L. - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Mar. 21 (0.0)	7	5	78.6	75.2	75.0	75.2	75.9	80.4
	8	4	67.5	60.5	60.0	60.5	62.0	71.3
	9	3	57.2	45.9	45.0	45.9	48.4	63.0
	10	2	48.4	31.5	30.0	31.5	35.5	56.2
	11	1	42.3	18.0	15.0	18.0*	24.8	51.6
	12		40.0	10.0	0.0	10.0	20.0	50.0
	am	pm	Horiz.	L. - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Apr. 21 (+11.9)	6	6	82.6	88.0	90.0	92.0	93.9	98.9
	7	5	71.1	73.5	75.3	77.6	80.2	89.5
	8	4	59.7	58.9	60.7	63.4	67.0	80.7
	9	3	48.7	44.2	46.2	49.7	54.4	73.1
	10	2	38.8	29.5	32.0	36.8	43.2	67.0
	11	1	31.3	14.8	18.9	26.2	34.9	63.0
	12		28.4	1.6	11.6	21.6	31.6	61.6
	am	pm	Horiz.	L. - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
May 21 (+20.3)	5	7	88.1	100.4	104.1	107.4	110.2	114.7
	6	6	77.3	86.6	90.0	93.4	96.7	105.2
	7	5	66.0	72.6	75.9	79.6	83.6	96.1
	8	4	54.6	58.5	62.0	66.2	71.1	87.7
	9	3	43.2	44.5	48.4	53.5	59.5	80.5
	10	2	32.5	30.6	35.5	42.1	49.6	74.9
	11	1	23.8	17.6	24.8	33.4	42.6	71.2
	12		20.0	10.0	20.0	30.0	40.0	70.0
	am	pm	Horiz.	L. - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jun. 21 (+23.45)	5	7	85.8	99.5	103.7	107.6	111.1	117.2
	6	6	75.2	86.0	90.0	94.0	97.8	107.7
	7	5	64.0	72.4	76.3	80.5	85.0	98.8
	8	4	52.6	58.6	62.7	67.5	72.8	90.6
	9	3	41.2	44.9	49.6	55.3	61.7	83.6
	10	2	30.2	31.6	37.4	44.5	52.4	78.1
	11	1	20.8	19.6	27.6	36.5	45.8	74.6
	12		16.6	13.4	23.4	33.4	43.4	73.4

**Table B11 Latitude 48°N, Incident Angles for Horizontal and South-Facing Tilted Surfaces**

Dates (Declination)	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Dec. 21 (-23.45)	9	3	82.0	55.3	49.6	44.9	41.8	41.6
	10	2	76.4	44.5	37.4	31.6	28.0	31.1
	11	1	72.7	36.5	27.6	19.6	14.3	22.4
	12		71.4	33.4	23.4	13.5	3.5	18.5
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jan. 21 (-19.9)	8	4	86.5	66.2	62.0	58.5	56.0	54.7
	9	3	79.0	53.5	48.4	44.5	42.2	43.7
	10	2	73.1	42.1	35.5	30.6	28.2	33.5
	11	1	69.3	33.4	24.8	17.6	14.1	25.4
Feb. 21 (-10.6)	12		68.0	30.0	20.0	10.0	0.0	22.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
7	5	87.6	77.2	75.2	73.7	72.6	72.2	
8	4	78.4	62.9	60.5	59.0	58.5	61.2	
Oct. 21 (-10.7)	9	3	70.3	49.0	45.9	44.3	44.5	50.7
	10	2	63.8	35.9	31.5	29.5	30.6	41.4
	11	1	59.5	25.0	18.0	14.8	17.6	34.6
	12		58.0	20.0	10.0	0.0	10.0	32.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Mar. 21 (0.0)	7	5	80.0	75.2	75.0	73.2	75.9	78.9
	8	4	70.5	60.5	60.0	60.5	62.0	68.2
	9	3	61.8	45.9	45.0	45.9	48.4	58.3
	10	2	54.6	31.5	30.0	31.5	35.5	49.9
Sep. 21 (0.0)	11	1	49.7	18.0	15.0	18.0	24.8	44.1
	12		48.0	10.0	0.0	10.0	20.0	42.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Apr. 21 (+11.9)	6	6	81.4	88.0	90.0	92.0	93.9	97.7
	7	5	71.4	73.5	75.3	77.6	80.2	86.9
	8	4	61.5	58.9	60.7	63.4	67.0	76.7
	9	3	52.2	44.2	46.2	49.7	54.4	67.7
Aug. 21 (+12.1)	10	2	44.2	29.5	32.0	36.8	43.2	60.3
	11	1	38.5	14.8	18.9	26.2	34.9	55.3
	12		36.4	1.6	11.6	21.6	31.6	53.6
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
May 21 (+20.3)	5	7	84.8	100.4	104.1	107.4	110.2	114.2
	6	6	75.3	86.6	90.0	93.4	96.7	103.2
	7	5	65.4	72.6	75.9	79.6	83.6	92.8
	8	4	55.4	58.5	62.0	66.2	71.1	83.1
Jul 21 (+20.5)	9	3	45.7	44.5	48.4	53.5	59.5	74.6
	10	2	37.0	30.6	35.5	42.1	49.6	67.9
	11	1	30.5	17.6	24.8	33.4	42.6	63.5
	12		28.0	10.0	20.0	30.0	40.0	62.0
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jun. 21 (+23.45)	5	7	82.1	99.5	103.7	107.6	111.1	116.3
	6	6	72.8	86.0	90.0	94.0	97.8	105.4
	7	5	63.0	72.4	76.3	80.5	85.0	95.2
	8	4	52.9	58.6	62.7	67.5	72.8	85.7
Jul 21 (+20.5)	9	3	43.1	44.9	49.6	55.3	61.7	77.5
	10	2	34.2	31.6	37.4	44.5	52.4	71.1
	11	1	27.3	19.6	27.6	36.5	45.8	66.9
	12		24.6	11.4	22.4	22.4	43.4	65.4

**Table B12 Latitude 56°N, Incident Angles for Horizontal and South-Facing Tilted Surfaces**

Dates (Declination)	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Dec. 21 (-23.45)	9	3	88.1	55.3	49.6	44.9	41.8	40.5
	10	2	83.4	44.5	37.4	31.6	28.0	28.2
	11	1	80.5	36.5	27.6	19.6	14.3	16.8
	12		79.4	33.4	23.4	13.5	3.4	10.5
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	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jan. 21 (-19.9)	9	3	85.0	53.5	48.4	44.5	42.2	42.1
	10	2	80.1	42.1	35.5	30.6	28.2	30.0
	11	1	77.1	33.4	24.8	17.6	14.1	19.3
	12		76.0	30.0	20.0	10.0	0.0	14.0
<hr/>								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Feb. 21 (-10.6)	8	4	82.5	62.9	60.5	59.0	58.5	59.6
	9	3	75.8	49.0	45.9	44.3	44.5	47.6
	10	2	70.6	35.9	31.5	29.5	30.6	36.5
	11	1	67.2	25.0	18.0	14.8	17.6	27.7
<hr/>								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Mar. 21 (0.0)	7	5	81.7	75.2	75.0	75.2	75.9	77.6
	8	4	73.9	60.5	60.0	60.5	62.0	65.0
	9	3	66.7	45.9	45.0	45.9	48.4	54.1
	10	2	61.0	31.5	30.0	31.5	35.5	44.1
<hr/>								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Apr. 21 (+11.9)	5	7	88.6	102.4	104.7	106.5	107.9	108.8
	6	6	80.4	88.0	90.0	92.0	93.9	96.5
	7	5	72.0	73.5	75.3	77.6	80.2	84.4
	8	4	63.9	58.9	60.7	63.4	67.0	72.9
<hr/>								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Aug. 21 (+12.1)	9	3	56.4	44.2	46.2	49.7	54.4	62.5
	10	2	50.1	29.5	32.0	36.3	43.2	53.8
	11	1	45.9	14.8	18.9	26.2	34.9	47.8
	12		44.4	1.6	11.6	21.6	31.6	45.6
<hr/>								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
May 21 (+20.3)	4	8	88.3	113.8	118.0	121.5	124.0	125.5
	5	7	81.5	100.4	104.1	107.4	110.2	113.1
	6	6	73.5	86.6	90.0	93.4	96.7	101.0
	7	5	65.2	72.6	75.9	79.6	83.6	89.4
<hr/>								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jul. 21 (+20.5)	8	4	56.9	58.5	62.0	66.2	71.1	78.6
	9	3	49.1	44.5	48.4	53.5	59.5	68.9
	10	2	42.4	30.6	35.5	42.1	49.6	61.1
	11	1	37.7	17.6	24.8	33.4	42.6	55.9
<hr/>								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jun. 21 (+23.45)	12		36.0	10.0	20.0	30.0	40.0	54.0
<hr/>								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jun. 21 (+23.45)	4	8	85.8	112.5	117.3	121.4	124.6	127.1
	5	7	78.6	99.5	103.7	107.6	111.1	114.8
	6	6	70.7	86.0	90.0	94.0	97.8	102.9
	7	5	62.4	72.4	76.3	80.5	85.0	91.5
<hr/>								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jun. 21 (+23.45)	8	4	54.1	58.6	62.7	67.5	72.8	80.9
	9	3	46.2	44.9	49.6	55.3	61.7	71.6
	10	2	39.3	31.6	37.4	44.5	52.4	64.1
	11	1	34.4	19.6	27.6	36.5	45.8	59.2
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	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jun. 21 (+23.45)	12		32.6	13.4	23.4	33.4	43.4	57.4

**Table B13 Latitude 64°N, Incident Angles for Horizontal and South-Facing Tilted Surfaces**

Dates (Declination)	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.



Dec. 21 (-23.45)	11	1	88.2	36.5	27.6	19.6	14.3	13.9
	12		87.4	33.4	23.4	13.5	3.4	2.5
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jan. 21 (-19.9)	10	2	87.2	42.1	35.5	30.6	28.2	28.2
	11	1	84.8	33.4	24.8	17.6	14.1	15.0
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Nov. 21 (-19.9)	10	2	87.2	42.1	35.5	30.6	28.2	28.2
	11	1	84.0	30.0	20.0	10.0	0.0	6.0
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Feb. 21 (-10.6)	8	4	86.6	62.9	60.5	59.0	58.5	58.3
	9	3	81.4	49.0	45.9	44.3	44.5	45.4
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Oct. 21 (-10.7)	10	2	77.4	35.9	31.5	29.5	30.6	32.6
	11	1	74.9	25.0	18.0	14.8	17.6	21.4
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Mar. 21 (0.0)	7	5	83.5	75.2	75.0	75.2	75.9	76.5
	8	4	77.3	60.5	60.0	60.5	62.0	63.3
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Sep. 21 (0.0)	9	3	71.9	45.9	45.0	45.9	48.4	50.5
	10	2	67.7	31.5	30.0	31.5	35.5	38.9
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Apr. 21 (+11.9)	5	7	86.0	102.4	104.7	106.5	107.9	108.4
	6	6	79.6	88.0	90.0	92.0	93.9	95.1
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Aug. 21 (+12.1)	7	5	73.0	73.5	75.3	77.6	80.2	82.0
	8	4	66.7	58.9	60.7	63.4	67.0	69.4
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
May 21 (+20.3)	9	3	61.0	44.2	46.2	49.7	54.4	57.7
	10	2	56.5	29.5	32.0	36.8	43.2	47.6
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jul. 21 (+20.5)	11	1	53.5	14.8	18.9	26.2	34.9	40.3
	12		52.4	1.6	11.6	21.6	31.6	37.6
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
May 21 (+20.3)	4	8	84.2	113.3	118.0	121.5	124.0	124.9
	5	7	78.4	100.4	104.1	107.4	110.2	111.6
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jul. 21 (+20.5)	6	6	72.1	86.6	90.0	93.4	96.7	98.6
	7	5	65.5	72.6	75.9	79.6	83.6	86.1
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jun 21 (+23.45)	8	4	59.1	58.5	62.0	66.2	71.1	74.2
	9	3	53.2	44.5	48.4	53.5	59.5	63.4
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jun 21 (+23.45)	10	2	48.4	30.6	35.5	42.1	49.6	54.4
	11	1	45.1	31.6	37.4	44.5	52.4	48.3
---								
	am	pm	Horiz.	L - 10	Lat.	Lat. + 10	Lat. + 20	Vert.
Jun 21 (+23.45)	12		40.6	13.5	23.4	33.4	43.4	49.4

**This Appendix is not part of this Standard but is included for information purposes only.**

**Appendix C**

This appendix presents a sample calculation showing how the test results obtained in accordance with this Standard can be used to compute the daily performance of a collector which is used for heating swimming pool water.

The collector considered is unglazed, south-facing and tilted at 30° with respect to the horizontal, and its efficiency is assumed to be described by Figure 4 in the body of the Standard. Its incident angle modifier is assumed to be described by the curve in Figure 5. For this example, the ambient temperature is assumed to vary from 15°C (59°F) to 27°C (81°F) during the day and the pool to have a constant temperature of 29°C (84°F). The location is 40°N latitude and the calculation is done for the 21st of September. Table C.1 shows the results of the calculation and each step is described as follows:

1. Inlet fluid temperature to the collector; this is assumed to be constant for all hours as described above.

2. Ambient air temperature; this assumed to vary as stated above and shown in Table C.1. If records of typical days are not available for the location of interest, a diurnal temperature profile can be calculated for the summer months based on Table 1, pg 24.4, and Table 3, pg 26.7 of reference 2.

3. Incident radiation on the collector plane; these values were taken for Table B4 for September 21, 30° tilt angle. Therefore this calculation is based on clear sky conditions. If only incident radiation on a horizontal surface is available for the location of interest, see reference 21, pp. 48-55 for procedures for converting the values to incident radiation on a tilted surface.

4.  $(t_{f,i} - t_a)/I_i$ ; these values were computed using the data from lines 1, 2, and 3.

5. Collector thermal efficiency at normal incidence; based on the calculated values in line 4, the collector efficiency was determined using Figure C.1 (duplicate of Figure 4).

6. Incident angle between the direct solar beam and outward drawn normal to the collector plane; these values were taken from Table B10 for September 21, L-10. To compute the values in general, see reference 21, pp. 14-18.

7. Incident angle modifier; although the incident angle modifier was only obtained for angles up to 60° as shown in Figure 5, for this example it was assumed to be constant and equal to 1.0 out to 75°. In reality, the incident angle modifier will drop off to values less than 1.0 between 60° and 75°; however, the collector efficiency is zero for the low radiation levels that occur at these angles. (Less than 5% of the daily total radiation falls at angles greater than 60°.)

8. Energy output from the collector; this is calculated using the equation shown.  $F_R(\tau\alpha)_{e,n}$  is obtained from the ordinate (y) intercept of Figure C.1 (Figure 4). For this example, since  $K_{air} \equiv 1$ , the energy output for all hours is simply the collector efficiency (expressed as a fraction) at normal incidence multiplied by the incident solar radiation.

9. Collector thermal efficiency; this is calculated using the equation shown. The approximate daily collector efficiency is obtained by dividing the daily total in line 8 by that in line 3. Since the values in the table are only rates and not hourly totals, the exact daily collector efficiency is obtained by plotting the curves shown in Figure C.2 using the hourly rates, determining the area under each curve, and calculating the ratio of the two areas.

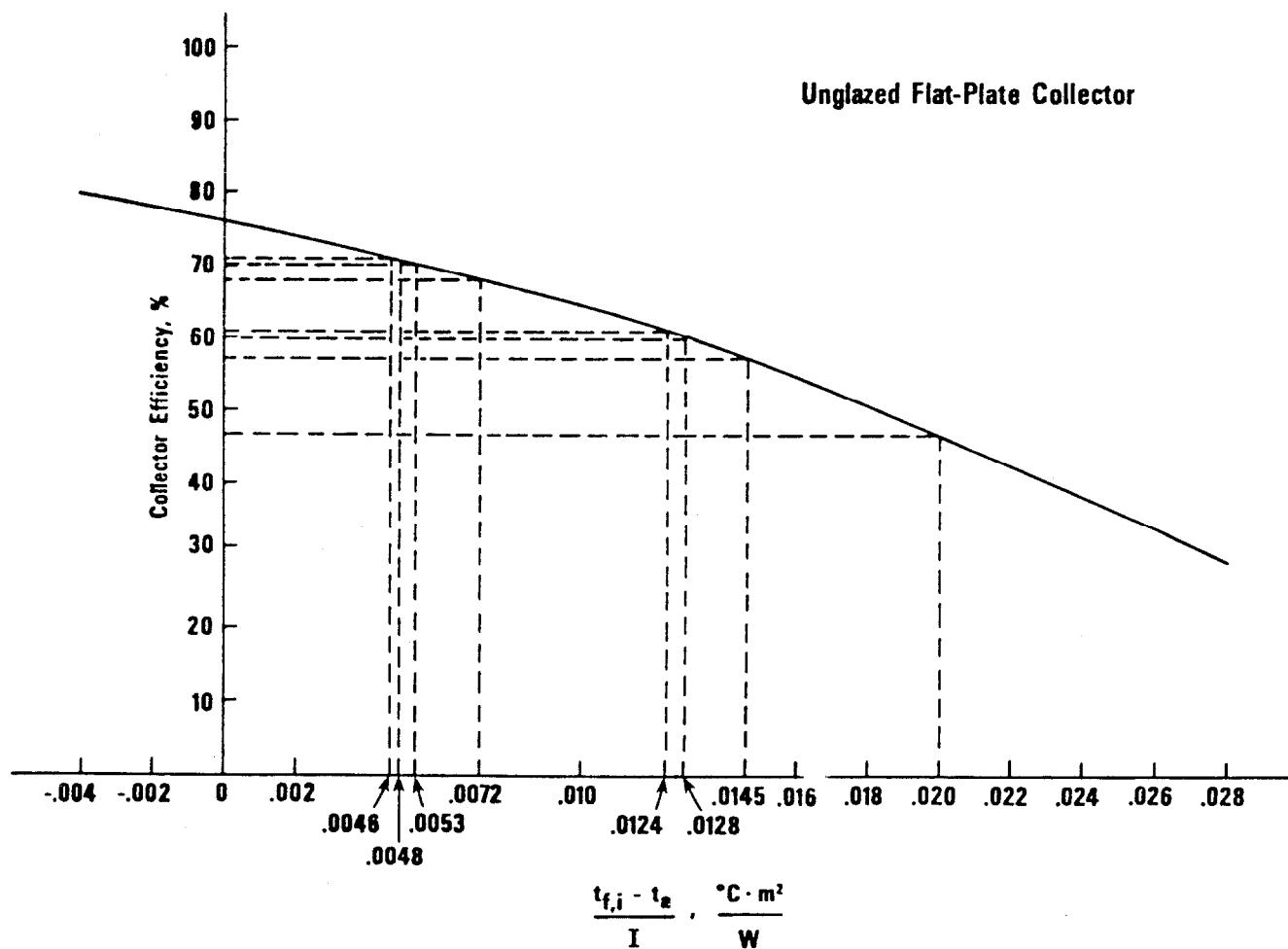


Figure C.1 Thermal Efficiency Curve Used in the Example Calculation

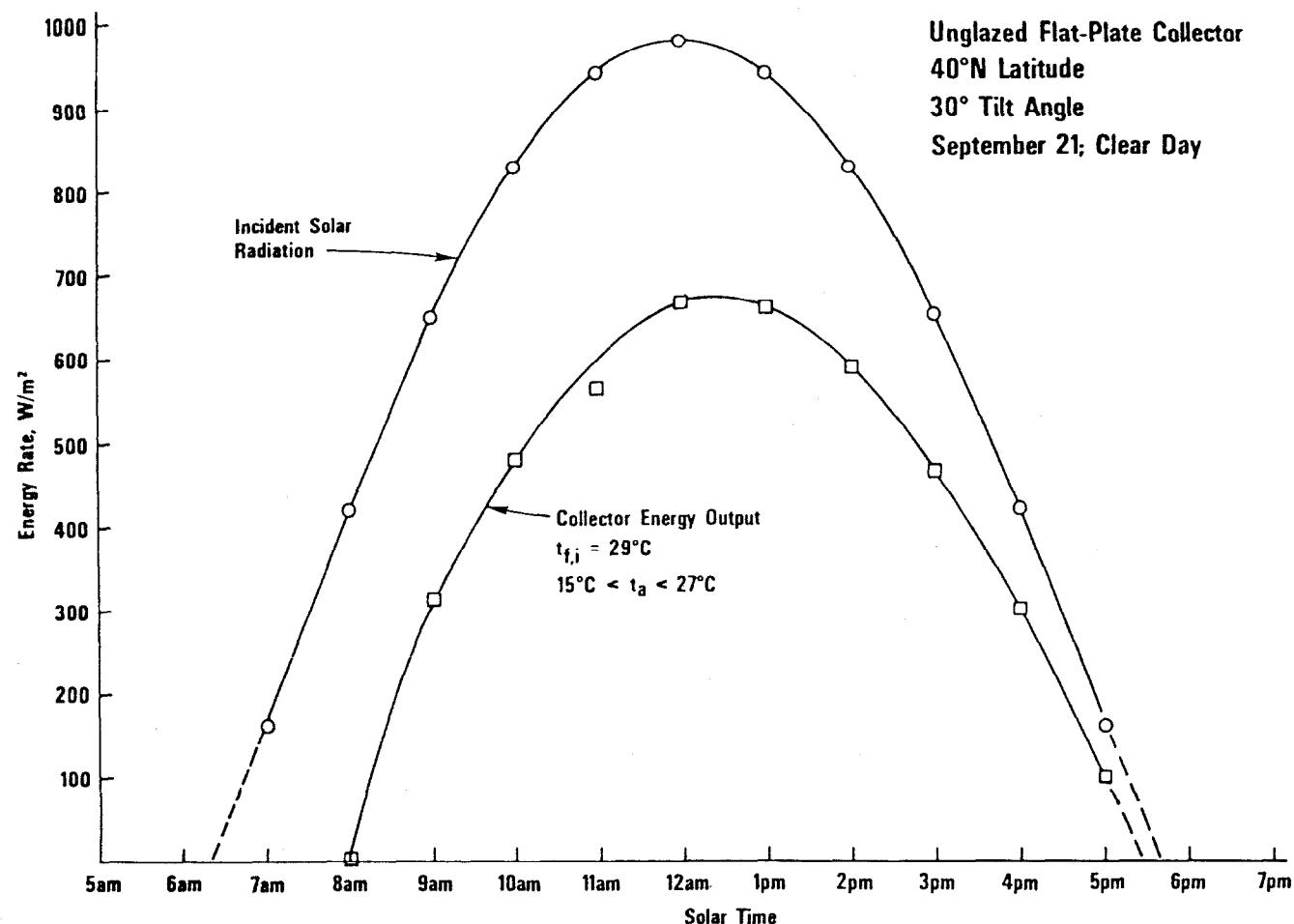


Figure C.2 Incident Solar Radiation and Solar Collector Output for the Example Calculation

Table B1 Solar Position and Insolation\* Values for 24 Degrees North Latitude

	7 am	8 am	9 am	10 am	11 am	12	1 pm	2 pm	3 pm	4 pm	5 pm	Daily Total
1. Inlet fluid temperature to the collector, $t_{f,i}$ , °C	29	29	29	29	29	29	29	29	29	29	29	—
2. Ambient air temperature, $t_a$ , °C	15	15	16	17	17	22	24	25	26	27	27	—
3. Incident radiation on the collector plane, $I_t$ , W/m²	161	419	649	826	939	977	939	826	649	419	161	6965
4. $(t_{f,i} - t_a)/I_t$ , (°C · m²)/W	0.0870	0.0334	0.0200	0.0145	0.0128	0.0072	0.0053	0.0048	0.0046	0.0048	0.0124	—
5. Collector thermal efficiency at normal incidence, fraction	0.0	0.0	0.48	0.58	0.60	0.68	0.70	0.71	0.71	0.71	0.61	—
6. Incident angle between the direct solar beam and outward drawn normal to the collector plane, °	75.2	60.5	45.9	31.5	18.0	10.0	18.0	31.5	45.9	60.5	75.2	—
7. Incident angle modifier, $K_{\alpha\tau}$	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	—
8. Energy output from the collector, W/m², line 3 [line 5 + $F_R (\tau\alpha)_{e,n} (K_{\alpha\tau} - 1)$ ]	0	0	312	479	563	644	657	586	461	297	98	4117
9. Collector thermal efficiency, fraction, line 8/line 3	0.0	0.0	0.48	0.58	0.60	0.68	0.70	0.71	0.71	0.71	0.61	0.59

## **POLICY STATEMENT DEFINING ASHRAE'S CONCERN FOR THE ENVIRONMENTAL IMPACT OF ITS ACTIVITIES**

ASHRAE is concerned with the impact of its members' activities on both the indoor and outdoor environment. ASHRAE's members will strive to minimize any possible deleterious effect on the indoor and outdoor environment of the systems and components in their responsibility while maximizing the beneficial effects these systems provide, consistent with accepted standards and the practical state of the art.

ASHRAE's short-range goal is to ensure that the systems and components within its scope do not impact the indoor and outdoor environment to a greater extent than specified by the standards and guidelines as established by itself and other responsible bodies.

As an ongoing goal, ASHRAE will, through its Standards Committee and extensive technical committee structure, continue to generate up-to-date standards and guidelines where appropriate and adopt, recommend, and promote those new and revised standards developed by other responsible organizations.

Through its *Handbook*, appropriate chapters will contain up-to-date standards and design considerations as the material is systematically revised.

ASHRAE will take the lead with respect to dissemination of environmental information of its primary interest and will seek out and disseminate information from other responsible organizations that is pertinent, as guides to updating standards and guidelines.

The effects of the design and selection of equipment and systems will be considered within the scope of the system's intended use and expected misuse. The disposal of hazardous materials, if any, will also be considered.

ASHRAE's primary concern for environmental impact will be at the site where equipment within ASHRAE's scope operates. However, energy source selection and the possible environmental impact due to the energy source and energy transportation will be considered where possible. Recommendations concerning energy source selection should be made by its members.

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